

# **COMPUTER SIMULATION OF EQUILIBRIUM MULTICOMPONENT MULTISTAGE SEPARATION PROCESSES**

**A Thesis Submitted  
In Partial Fulfilment of the Requirements  
for the Degree of  
MASTER OF TECHNOLOGY**

**by  
SAHIDUL ISLAM**

**to the**

**DEPARTMENT OF CHEMICAL ENGINEERING  
INDIAN INSTITUTE OF TECHNOLOGY KANPUR  
MAY, 1985**

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CERTIFICATE

This is to certify that the work presented in  
this thesis entitled, " COMPUTER SIMULATION OF EQUILIBRIUM  
MULTICOMPONENT MULTISTAGE SEPARATION PROCESSES " has been  
carried out by Mr. Sahidul Islam under my supervision and  
the same has not been submitted elsewhere for a degree.

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ACKNOWLEDGEMENT

I feel pleasure to express my deep appreciation to Dr. D.P. Rao for his invaluable help for the completion of this thesis.

I would be extremely happy to convey my sincere thanks to all my friends and seniors in different fields who helped me directly and indirectly for the completion of this thesis. Special thanks are due to Dr. Ratan Mohan, Dr. A.K. Verma, Mr. Raghu Raman, Mr. Mrityunjoy Chakroborty, Mr. Binoy Bhushan Kandir, Dr. Sujit Dutta, Mr. Susil Mandal, Mr. Kausik Banerjee, Mr. Tapas Mandal, Mr. S.R. Diksitulu, Mr. Alok Pandit, Mr. VLN Murthy, Mr. Saibal Banerjee, Mr. M.M. Beg, Dr. P.K. Bhatt and Miss Arti Gupta.

I do not know how I will express my deep appreciation to our immortal beloved Newton. As a child I am trying to understand and to apply one of his principle, which is nothing compare to his major contributions, but is the heart of this thesis.

Finally what I feel that help and inspiration is as if solely from \* Marrya who boosted me and thereby helping me to think the problem, has been inducing and driving me to my ultimate long desire.

Sahidul Islam

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ABSTRACT

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Month & Year of submission: May 1985  
Title of the Thesis : Computer Simulation of Equilibrium  
Multicomponent Multistage Separation  
Processes  
Thesis Supervisor : Dr. D.P. Rao

The modified Thomas algorithm is employed to obtain the correction vector  $\Delta \bar{X}$  in the widely used Naphthalis-Sandholm method of solving separation processes problems. An efficient algorithm for obtaining the correction  $\Delta \bar{X}$  is proposed in which the sparsity of the submatrices of the Jacobian has been exploited in the matrix multiplication and inversion. The operation count for the proposed algorithm and the standard matrix multiplication and inversion has been presented using two bench-mark problems. It has been shown that the use of the proposed algorithm results in considerable saving in the CPU time with increase in the number of components and stages. The proposed algorithm can be used for the extensions and variants of Naphthalis-Sandholm methods.

## CHAPTER 1

### INTRODUCTION

The classical techniques of separation of multicomponent mixtures like distillation, absorption, extraction, etc. are widely used in chemical industries. The design or simulation of these (stage-wise) separation processes involves the solution of the material and energy balance equations and equilibrium relations for each stage, and requires an enormous amount of computational effort. Before the widespread use of computers, short-cut methods were employed for the design though these are generally inadequate for systems other than the ones for which the equilibrium relations are linear. But with accessibility to powerful computers, the rigorous methods got impetus and several methods have been proposed.

The rigorous methods of design or simulation involve two major steps; namely formulation of basic equations and their numerical methods of solution. The methods of formulation of the basic equations, in turn, can be classified as component-wise grouping of variables and stage-wise grouping of variables. The earlier methods of solution like the B-P method, the sum-rate method and the relaxation technique can be visualized as the direct substitution methods. Recently, these methods of

solution have given way to the more efficient Newton-Raphson method and its variants.

Under the component-wise grouping of variables, the basic equations can be obtained as

$$\overset{=}{C}_i \overset{=}{X}_i = -\overset{=}{F}_i \quad \text{for } i = 1, 2, \dots, C \quad (1)$$

for the steady state conditions; where  $\overset{=}{C}_i$  is the coefficient matrix involving vapor and liquid flow rates and the k-values,  $\overset{=}{X}_i$  could be either liquid or vapor mole fractions or component flow rates,  $\overset{=}{F}_i$  are the feed component flow rates and i the components. In the relaxation technique (also known as False-Transient method) the basic equations are cast as

$$\overset{=}{C}_i^{k+1} \overset{=}{X}_i^{k+1} = \overset{=}{X}_i^k \quad i = 1, 2, \dots, C \quad (2)$$

where k is the iteration number.

More generally, the basic equations may be represented as

$$\overset{=}{A}_i \overset{=}{X}_i = \overset{=}{B}_i \quad i = 1, 2, \dots, C \quad (3)$$

The square matrix has the tridiagonal structure and  $\overset{=}{X}_i$  can be found using the well known Thomas algorithm.

Equation (3) together with the enthalpy balance equations around the stages can be solved by the direct

substitution method for any assumed liquid and vapor flow rates and temperatures. The B-P method, the sum-rate method and the modified relaxation technique fall under this category.

Since the year 1965, the direct substitution methods gave way to the Newton-Raphson method(or its modified versions) of solution. In these methods, the material balance discrepancy functions,

$$M_n = \sum_{i=1}^C y_{i,n} - \sum_{i=1}^C x_{i,n} \quad n = 1, 2, \dots, N \quad (4)$$

and the enthalpy discrepancy functions around each stage are expanded in the Taylor series. Assuming the second and higher order terms to be negligible, the equations are rearranged to obtain

$$\overset{=}{J} \Delta \overset{-}{X} = \overset{-}{b} \quad (5)$$

where  $\overset{=}{J}$  is the Jacobian matrix of  $2N \times 2N$ .

Several convergence schemes and the methods of obtaining the correction vector have been proposed. These have been discussed by Holland (2).

Naphthali (4) and later Naphthali and Sandholm (5) showed that the convergence characteristics are better if the stage-wise grouping of variables together with the Newton-Raphson method are employed. For each of the stages the

variables are the component liquid flow rates, temperature and the component vapor flow rates (i.e.  $l_i, T, v_i$ ). The component and the enthalpy discrepancy functions are formulated to yield

$$\mathbf{F}(\bar{\mathbf{x}}) = 0$$

Applying the Newton-Raphson technique we get

$$J \overset{=}{\Delta} \bar{\mathbf{x}} = -\mathbf{F}$$

The Jacobian is of the order  $(2C+1) N \times (2C+1)N$  and it has the block tridiagonal form. Several methods proposed for solving the separation problems deal with the techniques of obtaining the correction vector, Stadther [6, 7, 8].

It has been generally accepted that the Naphthali-Sandholm method has better convergence characteristics. However, it is likely to diverge if the guessed component liquid and vapor flow rates and temperatures are far from the correct values. To over come this problem, Ketchum [3] proposed the fusion of the relaxation technique and the Naphthali-Sandholm method and demonstrated its suitability for even interlinked columns. Later Hofeling and Seader [1] have demonstrated as to how the modified Thomas algorithm can be used for the interlinked columns. Stadther [6, 7, 8] has compared the

convergence characteristics of the modified Thomas algorithm and the other methods of solution using the sparse matrix technique. He finds the Thomas algorithm as good as the other sparse matrix techniques.

From the literature, it appears that the sparsity of the submatrices (diagonal and its adjacent submatrix) has not been exploited. The objective of the present work is to propose a more efficient method of solution taking advantage of the sparsity of the submatrices.

In Chapter 2, the method of formulation of the basic equations and the method of solution is presented. The results and discussion are presented in Chapter 3. Next conclusions is presented.

## CHAPTER 2

BASIC EQUATIONS AND METHOD OF SOLUTION

In this Chapter, the strategy of formulating the basic equations involving material and enthalpy balances, equilibrium and tray efficiency relations of multistage multicomponent separation processes, and the method of obtaining solution is presented.

A model of a general stage, along with the notation employed herein, is depicted in figure 1. The various discrepancy functions can be formulated as follows:

For Material balance:

$$M_{i,n} = l_{i,n-1} + v_{i,n+1} + f_{i,n} - (1+s_n)v_{i,n} - (1+s_n)l_{i,n} \quad (1)$$

$$\text{for } 1 \leq i \leq c \quad \& \quad 1 \leq n \leq N$$

where  $v_{i,n}$  and  $l_{i,n}$  are the flow rates of component  $i$  in liquid and vapor leaving the  $n$ th stage, and  $s_n v_n$  and  $s_n l_n$  are the vapor and liquid side streams drawn on the  $n$ th stage.

For Enthalpy balance:

$$E_n = \sum_{i=1}^c l_{i,n-1} h_{i,n-1} + \sum_{i=1}^c v_{i,n+1} h_{i,n+1} + \sum_{i=1}^c f_{i,n} h_{F_{i,n}} - \sum_{i=1}^c (1+s_n)v_{i,n} h_{i,n} - \sum_{i=1}^c (1+s_n)l_{i,n} h_{i,n} + q_n \dots \quad (2)$$

$$\text{for } 1 \leq i \leq c \quad \& \quad 1 \leq n \leq N$$

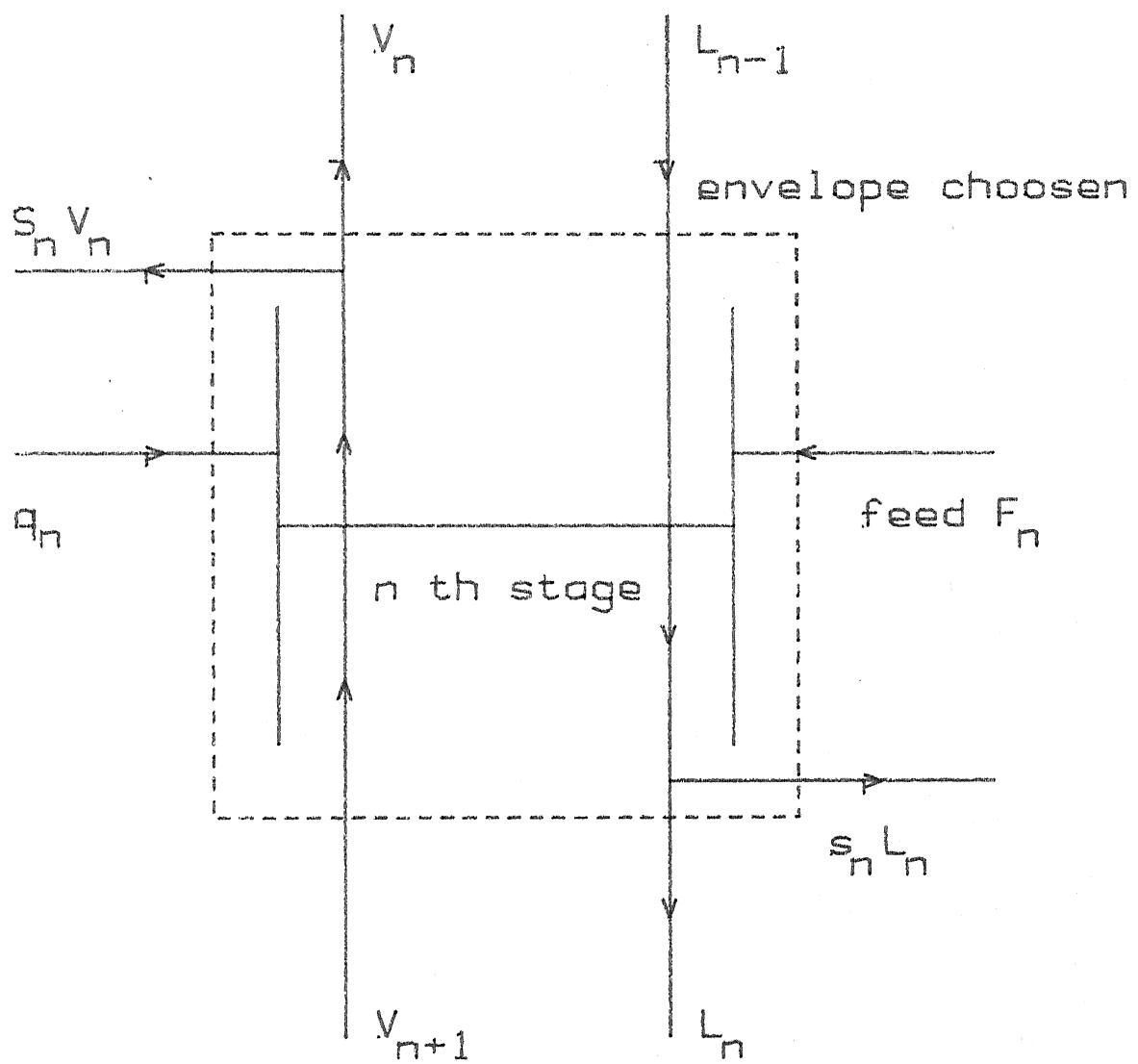


Fig. 1: A typical contacting stage

Equilibrium relations together with the Murphree efficiency:

$$o_{i,n} = \frac{\gamma_n k_{i,n} l_{i,n}}{L_n} - \frac{v_{i,n}}{v_n} + (1 - \gamma_n) \frac{v_{i,n+1}}{v_{n+1}} \dots \quad (3)$$

for  $1 \leq i, j \leq C$  &  $1 \leq n \leq N$

$$\text{where } \gamma_n = \frac{y_{i,n} - y_{i,n+1}}{k_{i,n} x_{i,n} - y_{i,n+1}} \dots \quad (3a)$$

Thus, there are  $N(2C+1)$  set of nonlinear equations and they have, to be solved to obtain the  $N(2C+1)$  unknown variables, namely

$l_{i,n}$ ,  $v_{i,n}$  and  $T_n$ .

The set of equations may be compactly written as

$$\bar{F} = \bar{F}(\bar{X}) = \bar{0} \quad (4)$$

where

$$\bar{F} = \left[ \bar{F}_1, \bar{F}_2, \dots, \bar{F}_n, \dots, \bar{F}_N \right]^T, \quad (5)$$

$$F_n = \left[ M_{1,n}, M_{2,n}, \dots, M_{C,n}, o_{1,n}, o_{2,n}, \dots, o_{C,N}, E_n \right]^T \quad (6)$$

$$\bar{X} = \left[ \bar{x}_1, \bar{x}_2, \dots, \bar{x}_m \right]^T \quad (7)$$

$$\text{and } \bar{X}_n = \left[ l_{1,n}, l_{2,n}, \dots, l_{C,n}, v_{1,n}, v_{2,n}, \dots, v_{C,n}, T_n \right]^T \quad (8)$$

It may be pointed out that the ordering of the variables is slightly different from the one proposed by Naphthali and

Sandholm 1971 . The reasons for the order chosen here is explained later.

Employing the Newton-Raphson technique, from Equation(4) we can obtain

$$\Delta \bar{X} = - \frac{\partial \bar{F}}{\partial \bar{X}}^{-1} \cdot \bar{F}$$

$$= - J^{-1} \cdot \bar{F}$$

where  $\bar{J}$  is the Jacobian matrix.

The Jacobian has the block tridiagonal structure and can be represented as

$$\bar{J} = \begin{bmatrix} \bar{B}_1 & \bar{C}_1 & & & \\ \bar{A}_2 & \bar{B}_2 & \bar{C}_2 & & \\ & \bar{A}_3 & \bar{B}_3 & \bar{C}_3 & \\ & & \ddots & \ddots & \ddots \\ & & & \bar{A}_n & \bar{B}_n & \bar{C}_n \\ & & & & \ddots & \ddots \\ & & & & & \bar{B}_N & \bar{C}_N \end{bmatrix}$$

where

$$\bar{A}_n = \frac{\partial \bar{F}_n}{\partial \bar{X}_{n-1}}, \quad \bar{B}_n = \frac{\partial \bar{F}_n}{\partial \bar{X}_n} \quad \text{and} \quad \bar{C}_n = \frac{\partial \bar{F}_n}{\partial \bar{X}_{n+1}}$$

and the rest of the elements are null matrices.

In expand form, the submatrix  $\bar{A}_n$  is

$$\bar{A}_n = \begin{bmatrix} \frac{\partial M_{1,n}}{\partial l_{1,n-1}}, \frac{\partial M_{1,n}}{\partial l_{2,n-1}}, \dots, \frac{\partial M_{1,n}}{\partial l_{C,n-1}}, \dots, \frac{\partial M_{1,n}}{\partial v_{1,n-1}}, \frac{\partial M_{1,n}}{\partial v_{2,n-1}}, \dots, \frac{\partial M_{1,n}}{\partial v_{C,n-1}}, \dots, \frac{\partial M_{1,n}}{\partial T_{n-1}} \\ \frac{\partial M_{2,n}}{\partial l_{1,n-1}}, \frac{\partial M_{2,n}}{\partial l_{2,n-1}}, \dots, \frac{\partial M_{2,n}}{\partial l_{C,n-1}}, \dots, \frac{\partial M_{2,n}}{\partial v_{1,n-1}}, \frac{\partial M_{2,n}}{\partial v_{2,n-1}}, \dots, \frac{\partial M_{2,n}}{\partial v_{C,n-1}}, \dots, \frac{\partial M_{2,n}}{\partial T_{n-1}} \\ \dots \quad \dots \\ \dots \quad \dots \\ \frac{\partial M_{C,n}}{\partial l_{1,n-1}}, \frac{\partial M_{C,n}}{\partial l_{2,n-1}}, \dots, \frac{\partial M_{C,n}}{\partial l_{C,n-1}}, \dots, \frac{\partial M_{C,n}}{\partial v_{1,n-1}}, \dots, \frac{\partial M_{C,n}}{\partial v_{2,n-1}}, \dots, \frac{\partial M_{C,n}}{\partial v_{C,n-1}}, \dots, \frac{\partial M_{C,n}}{\partial T_{n-1}} \\ \frac{\partial o_{1,n-1}}{\partial l_{1,n-1}}, \frac{\partial o_{1,n-1}}{\partial l_{2,n-1}}, \dots, \frac{\partial o_{1,n-1}}{\partial l_{C,n-1}}, \frac{\partial o_{1,n-1}}{\partial v_{1,n-1}}, \frac{\partial o_{1,n-1}}{\partial v_{2,n-1}}, \dots, \frac{\partial o_{1,n-1}}{\partial v_{C,n-1}}, \frac{\partial o_{1,n-1}}{\partial T_{n-1}} \\ \dots \quad \dots \\ \dots \quad \dots \\ \frac{\partial o_{C,n-1}}{\partial l_{1,n-1}}, \frac{\partial o_{C,n-1}}{\partial l_{2,n-1}}, \frac{\partial o_{C,n-1}}{\partial l_{C,n-1}}, \frac{\partial o_{C,n-1}}{\partial v_{1,n-1}}, \frac{\partial o_{C,n-1}}{\partial v_{2,n-1}}, \dots, \frac{\partial o_{C,n-1}}{\partial v_{C,n-1}}, \frac{\partial o_{C,n-1}}{\partial T_{n-1}} \\ \frac{\partial E_n}{\partial l_{1,n-1}}, \frac{\partial E_n}{\partial l_{2,n-1}}, \frac{\partial E_n}{\partial l_{C,n-1}}, \frac{\partial E_n}{\partial v_{1,n-1}}, \dots, \frac{\partial E_n}{\partial v_{C,n-1}}, \frac{\partial E_n}{\partial T_{n-1}} \end{bmatrix}$$

or,

$$= \begin{bmatrix} I_C & \bar{0}_C & \bar{0}_C \\ \bar{0}_C & \bar{0}_C & \bar{0}_C \\ \bar{h}_C & \bar{0}_C & C_{PL} \end{bmatrix}$$

where  $I$ ,  $\bar{0}$ ,  $\bar{h}$  are identity matrix, null matrix and null vector respectively. Subscript  $C$  indicates the dimension of the matrix or vector.  $\bar{h}$  is the liquid enthalpy vector ( $h_i$ ,  $i=1, C$ ) and  $C_{PL}$  is heat capacity of  $L_{n-1}$ .

In expanded form, the submatrix  $\overset{=}{B}_n$  is

$$\overset{=}{B}_m = \begin{bmatrix} \frac{\partial M_{1,n}}{\partial l_{1,n}}, \frac{\partial M_{1,n}}{\partial l_{2,n}}, \dots, \frac{\partial M_{1,n}}{\partial l_{C,n}}, \frac{\partial M_{1,n}}{\partial v_{1,n}}, \dots, \frac{\partial M_{1,n}}{\partial v_{C,n}}, \frac{\partial M_{1,n}}{\partial T_n} \\ \frac{\partial M_{2,n}}{\partial l_{1,n}}, \frac{\partial M_{2,n}}{\partial l_{2,n}}, \dots, \frac{\partial M_{2,n}}{\partial l_{C,n}}, \frac{\partial M_{2,n}}{\partial v_{1,n}}, \dots, \frac{\partial M_{2,n}}{\partial v_{C,n}}, \frac{\partial M_{2,n}}{\partial T_n} \\ \dots \quad \dots \quad \dots \quad \dots \quad \dots \quad \dots \quad \dots \\ \dots \quad \dots \quad \dots \quad \dots \quad \dots \quad \dots \quad \dots \\ \frac{\partial M_{C,n}}{\partial l_{1,n}}, \frac{\partial M_{C,n}}{\partial l_{2,n}}, \dots, \frac{\partial M_{C,n}}{\partial l_{C,n}}, \frac{\partial M_{C,n}}{\partial v_{1,n}}, \dots, \frac{\partial M_{C,n}}{\partial v_{C,n}}, \frac{\partial M_{C,n}}{\partial T_n} \\ \frac{\partial O_{1,n}}{\partial l_{1,n}}, \frac{\partial O_{1,n}}{\partial l_{2,n}}, \dots, \frac{\partial O_{1,n}}{\partial l_{C,n}}, \frac{\partial O_{1,n}}{\partial v_{1,n}}, \dots, \frac{\partial O_{1,n}}{\partial v_{C,n}}, \frac{\partial O_{1,n}}{\partial T_n} \\ \dots \quad \dots \quad \dots \quad \dots \quad \dots \quad \dots \quad \dots \\ \dots \quad \dots \quad \dots \quad \dots \quad \dots \quad \dots \quad \dots \\ \frac{\partial O_{C,n}}{\partial l_{1,n}}, \frac{\partial O_{C,n}}{\partial l_{2,n}}, \dots, \frac{\partial O_{C,n}}{\partial l_{C,n}}, \frac{\partial O_{C,n}}{\partial v_{1,n}}, \dots, \frac{\partial O_{C,n}}{\partial v_{C,n}}, \frac{\partial O_{C,n}}{\partial T_n} \\ \frac{\partial E_n}{\partial l_{1,n}}, \frac{\partial E_n}{\partial l_{2,n}}, \dots, \frac{\partial E_n}{\partial l_{C,n}}, \frac{\partial E_n}{\partial v_{1,n}}, \dots, \frac{\partial E_n}{\partial v_{C,n}}, \frac{\partial E_m}{\partial T_n} \end{bmatrix}$$

and can be simplified to yield

$$\overline{B}_n = \begin{bmatrix} -(1+s_n) & \text{only diagonal element of block submatrix } -(1+s_n) \\ \vdots & \vdots \\ \overline{B}_n = & \vdots \\ \text{Totally filled submatrix} & \text{Totally filled submatrix} \\ h_1 & \dots & \dots & h_c & \dots & \dots & H_1 & \dots & \dots & \dots & H_C & \dots & * \end{bmatrix}$$

$$\text{or, } \overline{B}_n = \begin{bmatrix} -(1+s_n) & \overline{I}_C & (1+s_n) & \overline{I}_C & \overline{O}_C \\ & \overline{X}_C & & \overline{X}_C & \overline{X}_C \\ (1+s_n) & \overline{h}_C & (1+s_n) & \overline{H}_C & \overline{C}_{PLV} \end{bmatrix}$$

where  $\overline{X}$ ,  $\overline{X}$  and  $X$  denote the filled matrix, vector and nonzero element respectively and the subscript C the orders of the matrix or vector.

$$\begin{array}{|c}
 \hline
 \frac{\partial^M_{1,n}}{\partial^{I_1}_{1,n+1}}, \frac{\partial^M_{1,n}}{\partial^{I_2}_{2,n+1}} \dots \dots \frac{\partial^M_{1,n}}{\partial^{I_C}_{1,n+1}}, \frac{\partial^M_{1,n}}{\partial^{V_1}_{1,n+1}} \dots \frac{\partial^M_{1,n}}{\partial^{V_C}_{n+1}}, \frac{\partial^M_{1,n}}{\partial^T_{n+1}} \\
 \frac{\partial^M_{2,n}}{\partial^{I_1}_{1,n+1}}, \frac{\partial^M_{2,n}}{\partial^{I_2}_{2,n+1}} \dots \dots \frac{\partial^M_{2,n}}{\partial^{I_C}_{1,n+1}}, \frac{\partial^M_{2,n}}{\partial^{V_1}_{1,n+1}} \dots \frac{\partial^M_{2,n}}{\partial^{V_C}_{n+1}}, \frac{\partial^M_{2,n}}{\partial^T_{n+1}} \\
 \dots \dots \dots \dots \dots \dots \dots \dots \dots \\
 \dots \dots \dots \dots \dots \dots \dots \dots \dots \\
 \dots \dots \dots \dots \dots \dots \dots \dots \dots \\
 \hline
 \text{C}_n = \frac{\partial^M_{C,n}}{\partial^{I_1}_{1,n+1}}, \frac{\partial^M_{C,n}}{\partial^{I_2}_{2,n+1}} \dots \dots \frac{\partial^M_{C,n}}{\partial^{I_C}_{1,n+1}}, \frac{\partial^M_{C,n}}{\partial^{V_1}_{1,n+1}} \dots \frac{\partial^M_{C,n}}{\partial^{V_C}_{n+1}}, \frac{\partial^M_{C,n}}{\partial^T_{n+1}} \\
 \frac{\partial^O_{1,n}}{\partial^{I_1}_{1,n+1}}, \frac{\partial^O_{1,n}}{\partial^{I_1}_{1,n+1}} \dots \dots \frac{\partial^O_{1,n}}{\partial^{I_1}_{1,n+1}}, \frac{\partial^O_{1,n}}{\partial^{V_1}_{1,n+1}} \dots \frac{\partial^O_{1,n}}{\partial^{V_1}_{1,n+1}}, \frac{\partial^O_{1,n}}{\partial^T_{n+1}} \\
 \dots \dots \dots \dots \dots \dots \dots \dots \dots \\
 \dots \dots \dots \dots \dots \dots \dots \dots \dots \\
 \frac{\partial^O_{C,n}}{\partial^{I_1}_{1,n+1}}, \frac{\partial^O_{C,n}}{\partial^{I_2}_{2,n+1}} \dots \dots \frac{\partial^O_{C,n}}{\partial^{I_C}_{1,n+1}}, \frac{\partial^O_{C,n}}{\partial^{V_1}_{1,n+1}} \dots \frac{\partial^O_{C,n}}{\partial^{V_C}_{n+1}}, \frac{\partial^O_{C,n}}{\partial^T_{n+1}} \\
 \hline
 \frac{\partial^E_n}{\partial^{I_1}_{1,n+1}}, \frac{\partial^E_n}{\partial^{I_2}_{2,n+1}} \dots \dots \frac{\partial^E_n}{\partial^{I_C}_{1,n+1}}, \frac{\partial^E_n}{\partial^{V_1}_{1,n+1}} \dots \frac{\partial^E_n}{\partial^{V_C}_{n+1}}, \frac{\partial^E_n}{\partial^T_{n+1}}
 \end{array}$$

$$= C_n = \begin{bmatrix} & & \text{unit block} \\ & & \text{submatrix} \\ \text{null block matrix} & & \text{Totally filled} \\ & & \text{block sub matrix} \\ & H_{1,n+1} \cdots \cdots \cdots H_{C,n+1} & * \\ & & \end{bmatrix}$$

null column vector

and can be simplified to get

$$\begin{bmatrix} \bar{O}_C & \bar{I}_C & \bar{O}_C \\ \bar{O}_C & \bar{X}_C & \bar{O}_C \\ \bar{O}_C & \bar{H}_C & C_{AV} \end{bmatrix}$$

### THOMAS ALGORITHM

The correction vector  $\bar{X}$  can be found by the Thomas algorithm and is given below

Forward Substitution:

For the stage 1

$$\begin{aligned} \text{Steps: 1 } & \stackrel{=}{P}_1 \leftarrow (\stackrel{=}{B}_1)^{-1} \stackrel{=}{C}_1 \\ : 2 & \stackrel{=}{Q}_1 \leftarrow (\stackrel{=}{B}_1)^{-1} \stackrel{=}{F}_1 \end{aligned}$$

For the stages n from 2 to (N-1)

$$\begin{aligned} : 3 & \stackrel{=}{P}_n \leftarrow (\stackrel{=}{B}_n - \stackrel{=}{A}_n \stackrel{=}{P}_{n-1})^{-1} \stackrel{=}{C}_n \\ : 4 & \stackrel{=}{Q}_n \leftarrow (\stackrel{=}{B}_n - \stackrel{=}{A}_n \stackrel{=}{P}_{n-1})^{-1} (\stackrel{=}{F}_n - \stackrel{=}{A}_n \stackrel{=}{Q}_{n-1}) \end{aligned}$$

For the last stage N

$$: 5 \quad \stackrel{=}{Q}_N \leftarrow (\stackrel{=}{B}_N - \stackrel{=}{A}_N \stackrel{=}{P}_{N-1})^{-1} (\stackrel{=}{F}_N - \stackrel{=}{A}_N \stackrel{=}{Q}_{N-1})$$

Backward substitution

$$: 6 \quad \Delta \bar{X}_N \leftarrow \stackrel{=}{Q}_N$$

For the stages n from N-1 to 1

$$: 7 \quad \Delta \bar{X}_n \leftarrow -(\stackrel{=}{Q}_n - \stackrel{=}{P}_n \bar{X}_{n+1})$$

It can be seen that the algorithm involves several time taking matrix multiplications and inversions. Advantage of the sparsity and the structure of these matrices can be taken to minimise the machine operations, as described below.

In step 1 and 3, we encounter the matrix multiplications  $(\bar{B})^{-1} \bar{C}_1$  and  $(\bar{B}_j - \bar{A}_{j-1} \bar{P}_{j-1})^{-1} \bar{C}_j$ . The inverted matrices are totally filled while  $\bar{C}_1$  and  $\bar{C}_j$  are highly sparse. The structure of the resulting matrix is

$$\begin{array}{c} \text{Filled} \\ \text{matrix} \end{array} \left[ \begin{array}{ccc} = & = & = \\ = & \bar{0}_C & \bar{I}_C & \bar{0}_C \\ = & = & = \\ = & \bar{0}_C & \bar{X}_C & \bar{0}_C \\ = & = & = \\ \bar{0}_C & \bar{X}_C & X \end{array} \right] = \left[ \begin{array}{ccc} = & = & = \\ = & \bar{0}_C & \bar{X}_C & \bar{X}_C \\ = & = & = \\ = & \bar{0}_C & \bar{X}_C & \bar{X}_C \\ = & = & = \\ \bar{0}_C & \bar{X}_C & X \end{array} \right]$$

$$(\bar{B})^{-1} \text{ or } (\bar{B} - \bar{A}_{j-1} \bar{P}_{j-1})^{-1} \bar{C}_j \quad \bar{P}_j$$

where  $\bar{X}$ ,  $\bar{\bar{X}}$  and  $X$  denote the filled matrix, vector and non-zero element respectively,  $\bar{0}$  and  $\bar{I}$  are the null and identity matrices, and the subscript C the order of the matrix or vector.

It can be seen that there is no need to compute the elements of the first C columns of the resulting matrix and we can save  $C(2C+1)^2$  operations. Further, the next C columns can be found as

$$P_{j,C+i} = b_{j,i+C}^I + \sum_{k=C+1}^{2C+1} b_{j,k}^I c_{k,C+i} \quad \text{for } 1 \leq j \leq 2C+1 \quad 1 \leq i \leq C \quad (3)$$

The elements of the last column are

$$P_{j,2C+1} = b_{j,2C+1}^I c_{2C+1,2C+1} \quad (4)$$

Thus the operation count of this matrix multiplication is  $(C^2+1)(2C+1)$  instead of  $(2C+1)^3$  required for standard matrix multiplication.

The matrix multiplication  $A_j = P_{j-1} (= \alpha_j)$  carried out taking the advantage of sparsity as given below.

$$\left[ \begin{array}{ccc} = & = & = \\ I_C & O_C & \bar{O}_C \\ = & = & = \\ O_C & O_C & \bar{O}_C \\ \bar{h}_C & \bar{O} & C_{PL} \\ = & A_n \end{array} \right] \left[ \begin{array}{ccc} = & = & = \\ O_C & X_C & \bar{X}_C \\ = & = & = \\ O_C & X_0 & \bar{X}_C \\ \bar{X}_C & = & X \\ P_{n-1} & & \end{array} \right] = \left[ \begin{array}{ccc} = & = & = \\ O_C & X_C & \bar{X}_C \\ = & = & = \\ O_C & O_C & \bar{O}_C \\ \bar{O}_C & \bar{X}_C & X \\ = & \alpha_n & \end{array} \right] \quad (5)$$

Here, only the  $\bar{X}_C$ ,  $X$  in the row need to be computed.

The nonzero elements of  $\alpha_n^=$  are:

$$\alpha_{j,c+i} = p_{j,c+1} \quad \text{for } 1 \leq j \leq c+1 \quad (6)$$

$1 \leq i \leq c$

$$\alpha_{2c+1, c+i} = \sum_{k=1}^c A_{2c+1, k} p_{k, c+i} + A_{2c+1, 2c+1} p_{2c+1, c+i}$$

for  $1 \leq i \leq c+1$  (7)

Thus we need to perform only  $(C+1)^2$  scalar multiplication instead of  $(2C+1)^3$ .

The product  $\bar{A}_n \bar{F}_{n-1} = \bar{P}_{n-1}$  may be found as follows

$$\begin{bmatrix} \bar{I}_C & \bar{O}_C & \bar{O}_C \\ \bar{O}_C & \bar{O}_C & \bar{O}_C \\ \bar{H}_C & \bar{O}_C & C_{PL} \end{bmatrix} \begin{bmatrix} \bar{F}_0 \\ \bar{F}_0 \\ F \end{bmatrix} = \begin{bmatrix} \bar{F}_C \\ \bar{O}_C \\ f \end{bmatrix}$$

$$\bar{A} \quad \bar{F}$$

where  $\bar{P}_j = \bar{F}_j$  for  $1 \leq j \leq c$  (8)

$$\bar{P}_{2c+1} = \sum_{k=1}^c A_{2c+1,k} F_k + A_{2c+1,2c+1} F_{2c+1} \quad (9)$$

only the last element need to be computed; thus only  $c+1$  operations are required instead of  $(2c+1)^2$  operations for the standard matrix multiplication. In backward substitution, the multiplication  $P_n X_{n+1}$  involves  $(2c+1)(c+1)$  since the first  $c$  columns are zero elements.

Inversion of  $(\bar{B}_n - \bar{A}_n \bar{P}_{n-1})$  by partitioning.

Inversion by partitioning does not save the operations to be performed. But from the structure of the matrix  $(\bar{B}_n - \bar{A}_n \bar{P}_{n-1})$  some saving in operations can be realised as shown below.

$$(\bar{B}_n - \bar{A}_n \bar{P}_{n-1}) = \bar{b} =$$

$$\begin{bmatrix} (1+s_n) \bar{I}_C & \bar{x}_C & \bar{x}_C \\ \bar{x}_C & \bar{x}_C & \bar{x}_C \\ \bar{x}_C & \bar{x}_C & x \end{bmatrix}$$

$$= \begin{bmatrix} = b_{11} & \bar{b}_{12} \\ \bar{b}_{21} & b_{22} \end{bmatrix}$$

The inverse is given by

$$= b^{-1} = \begin{bmatrix} = D_{11} & \bar{D}_{12} \\ \bar{D}_{21} & D_{22} \end{bmatrix}$$

$$\text{where } = D_{11} = ( = b_{11})^{-1} + ( = b_{11})^{-1} \bar{b}_{12} D_{22} \bar{b}_{21} ( = b_{11})^{-1}$$

$$\bar{D}_{12} = - ( = b_{11})^{-1} \bar{b}_{12} D_{22}$$

$$\bar{D}_{21} = - D_{22} \bar{b}_{21} ( = b_{11})^{-1}$$

$$D_{22} = (b_{22} - \bar{b}_{21} ( = b_{11})^{-1} \bar{b}_{12})^{-1}$$

The inverse of  $= b_{11}$  can, in turn, be found by partitioning as given below.

$$= b_{11} = \begin{bmatrix} (1+s_n) = I_C & = X_C \\ = X_C & = X_C \end{bmatrix} = \begin{bmatrix} = d_{11} & = d_{12} \\ = d_{21} & = d_{22} \end{bmatrix}$$

$$( = b_{11})^{-1} = \begin{bmatrix} = e_{11} & = e_{12} \\ = e_{21} & = e_{22} \end{bmatrix}$$

where

$$\begin{aligned}\overset{=}{e}_{11} &= (\overset{=}{d}_{11})^{-1} + (\overset{=}{d}_{11})^{-1} \overset{=}{d}_{12} \overset{=}{e}_{22} \overset{=}{d}_{21} (\overset{=}{d}_{11})^{-1} \\ \overset{=}{e}_{12} &= -(\overset{=}{d}_{11})^{-1} \overset{=}{d}_{12} \overset{=}{e}_{22} \\ \overset{=}{e}_{21} &= -\overset{=}{e}_{22} \overset{=}{d}_{21} (\overset{=}{d}_{11})^{-1} \\ \overset{=}{e}_{22} &= (\overset{=}{d}_{22} - \overset{=}{d}_{21} (\overset{=}{d}_{11})^{-1} \overset{=}{d}_{12})^{-1}\end{aligned}$$

It may be noted  $\overset{=}{d}_{11}$  is a diagonal matrix and its inversion can be obtained by simply taking the reciprocal of each of the diagonal elements. Thus to find the inverse of a matrix of  $2C+1$ , we need only the standard inversion of matrix of order C and some matrix multiplications.

	Operation Count	Standard operation	Saving
$\sum_{j=1}^n$	$(C^2+1)(2C+1)$ $= 2C^3 + C^2 + 2C + 1$	$(2C+1)^3$ $= 8C^3 + 12C^2 + 6C + 1$	$6C^3 + 11C^2 + 4C$
$\sum_{j=1}^n$	$(C+1)^2$ $= C^2 + 2C + 1$	$8C^3 + 12C^2 + 6C + 1$	$8C^3 + 11C^2 + 4C + 1$
$\sum_{j=1}^n$	$(C+1)$	$(2C+1)^2$ $= 4C^2 + 4C + 1$	$4C^2 + 3C$
$\sum_{n=1}^{\infty}$	$x_n = 2C^2 + 3C + 1$	$4C^2 + 4C + 1$	$2C^2 + C$
Inv	$5C^3 + 14C^2 + 6C$	$8C^3 + 12C^2 + 6C + 1$	$3C^3 - 2C^2 + 1$
$\sum_{j=1}^n$	$(N-1)(2C^3 + C^2 + 2C + 1)$	$(N-1)(8C^3 + 12C^2 + 6C + 1)$	
$\sum_{j=1}^n$	$N(C^2 + 2C + 1)$	$N(8C^3 + 12C^2 + 6C + 1)$	
$\sum_{j=1}^n$	$N(C + 1)$	$N(4C^2 + 4C + 1)$	
$\sum_{n=1}^{\infty}$	$x_n = (N-1)(C^2 + 2C + 1)$	$(N-1)(4C^2 + 4C + 1)$	
Inv	$N(5C^3 + 14C^2 + 6C)$	$N(8C^3 + 12C^2 + 6C + 1)$	
Total count	$3N(5C^3 + 15C^2 + 9C + 2) + 2(N-1)(2C^3 + 2C^2 + 3C + 1)$	$3N(16C^3 + 28C^2 + 16C + 3) + 2(N-1)(8C^3 + 16C^2 + 10C + 2) + 7C + 1$	$3N(11C^3 + 13C^2 + 2C + 1) + 2(N-1)(6C^3 + 14C^2 + 7C + 1)$

## CHAPTER 3

RESULTS AND DISCUSSION

The algorithm proposed in the previous chapter has been implemented in FORTRAN 10 on the DEC 10 system. First, the saving in CPU time for inventing the matrix  $(\tilde{B}_n - \tilde{A}_{n,n-1} \tilde{C}_{n-1})$  has been examined. The efficiency of the proposed method has been tested by solving two absorption problems and the details are presented in this chapter.

It is known that the inversion of matrix by partition does not result in saving the CPU time. But, the structure matrix in these separation process problems is such that we need to invert only  $C \times C$  matrix to get the inversion of  $(2C+1) \times (2C+1)$ . This is so because the other submatrix, obtained on partitioning, whose inverse to be found is either identity matrix or a diagonal matrix with only a few elements which are other than one. Thus some CPU time saving can be achieved. As shown in the previous Chapter, the operation count for the inversion for a problem involving  $C$  components is  $(5C^3 + 14C^2 + 6C)$  compared the standard inversion (i.e. either by the Gaussian elemination or the Gauss-Jordon elimination) which is  $(2C+1)^3$ .

TABLE 2

SAMPLE PROBLEM NO.1 Taken from [3]

Absorption column having 20 plates and 4 component system

Component	Rich gas $v_{N+1,i}$ mole/hr	Absorbing liq. $l_{o,i}$ mole/hr	
A	75.0	0.0	
B	15.0	0.0	Absorbing liq. temp. = 125°C
C	10.0	0.0	Entering rich gas temp.=200°C
D	0.0	100.0	

Find the temperature and flow rates of the components of vapor and liquid stream leaving from the column.

TABLE 3  
SAMPLE PROBLEM No.2  
STATEMENT OF THE PROBLEM

COMPONENT	RICH GAS $v_{N+1,i}$ (mol/h)	Lean Oil $l_{o,i}$ (mol/h)	OTHER SPECIFICATIONS
$\text{CO}_2$	0.4703	0.0	$T_o = 2.9^\circ\text{F}$ , $T_{N+1} = 0^\circ\text{F}$ ,
$\text{N}_2$	0.1822	0.0	$N = 8$ , and
$\text{CH}_4$	88.7000	0.0	$P = 800 \text{ lb/in}^2 \text{ abs}$
$\text{C}_2\text{H}_6$	6.6747	0.0	initial temperature
$\text{C}_3\text{H}_8$	2.7786	0.0015	profile to be constant
i $\text{C}_4\text{H}_{10}$	0.6375	0.0006	at $T_j = 25^\circ\text{F}$
n $\text{C}_4\text{H}_{10}$	0.3655	0.0013	for all $j$ ( $j = 1, 2, \dots, N$ ).
i $\text{C}_5\text{H}_{12}$	0.1158	0.0067	The initial vapor rate
n $\text{C}_5\text{H}_{12}$	0.0505	0.0061	profile is to be constant
$\text{C}_6\text{H}_{14}$	0.0146	0.1495	at $v_j = 90.88$ ( $j = 1, 2, \dots, 8$ )
$\text{C}_7\text{H}_{16}$	0.0081	0.5736	and the liquid rates are
$\text{C}_8\text{H}_{18}$	0.002	1.8214	$L_j = 6.3095$ ( $j = 1, 2, \dots, 8$ )
$\text{C}_9\text{H}_{20}$	0.000	1.6866	and $L_8 = 15.42$
$\text{C}_{10}\text{H}_{22}$	0.000	2.0619	

TABLE -5

Table 5 (continued)

TEMPERATURE GUESS AREAS

Table 5 (continued)

PREDICTED MASS BALANCE = 0.8625E+02  
 $J_2 = 6$  - REPEL EJECTION = 0.1872E+11  
 INTERPOLATION = 1

PREDICTED MASS BALANCE = 0.2946E+11  
 $J_2 = 8$  - ATTRACTION = 0.6312E+05  
 INTERPOLATION = 2

PREDICTED MASS BALANCE = 0.2471E+11  
 $J_2 = 8$  - REPUL. EJECTION = 0.7273E+05  
 INTERPOLATION = 2

PREDICTED MASS BALANCE = 0.2617E+11  
 $J_2 = 8$  - REPUL. EJECTION = 0.5145E+03  
 INTERPOLATION = 1

PREDICTED MASS BALANCE = 0.1765E+11  
 $J_2 = 8$  - ATTRACTION = 0.8651E+03  
 INTERPOLATION = 1

PREDICTED MASS BALANCE = 0.4231E+11  
 $J_2 = 8$  - REPUL. EJECTION = 0.5946E+03  
 INTERPOLATION = 1

PREDICTED MASS BALANCE = 0.4231E+11  
 $J_2 = 8$  - REPUL. EJECTION = 0.5946E+03  
 INTERPOLATION = 1

PREDICTED MASS BALANCE = 0.4231E+11  
 $J_2 = 8$  - REPUL. EJECTION = 0.5946E+03  
 INTERPOLATION = 1

Table 5 (continued)

THE VALUES OF FINAL RATES AND TEMPERATURE ARE

**VARIOUS GRADES OF COPPERING FLOW RATES ARE**

CONTINUATION OF THE STAGES AND ADVICE

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Table 5 (continued)

VAPOR AND LIQUID RATE AND TEMPERATURE ARE

STRETCH RATIO	VAPOR RATE	LIQUID RATE	TEMPERATURE
1.0000000000000000	0.89923526E+02	0.10938037E+02	0.50106360E+03
1.0344827585572390	0.9343529538E+02	0.11248682E+02	0.50395584E+03
1.0699223172906402	0.94763597E+02	0.11502861E+02	0.50320764E+03
1.105400731558E+02	0.950172906402	0.11788229E+02	0.50124028E+03
1.140878333778E+02	0.953031558E+02	0.12156413E+02	0.49855777E+03
1.1763567778E+02	0.9567133778E+02	0.12701652E+02	0.49504246E+03
1.2118345778E+02	0.9592165778E+02	0.1336913E+02	0.49003263E+03
1.2472116338E+02	0.9617116338E+02	0.136484876E+02	0.48148252E+03

OUTPUT OF PROB. NO. 1

TABLE 6

Table 6 (continued)

STAGE NUMBER	COMPONENT NO.	COMPONENT RATE
1	DMP	VAP. RATE
2	W	W
3	W	W
4	W	W
5	W	W
6	W	W
7	W	W
8	W	W
9	W	W
10	W	W
11	W	W
12	W	W
13	W	W
14	W	W
15	W	W
16	W	W
17	W	W
18	W	W
19	W	W
20	W	W
21	W	W
22	W	W
23	W	W
24	W	W
25	W	W
26	W	W
27	W	W
28	W	W
29	W	W
30	W	W
31	W	W
32	W	W
33	W	W
34	W	W
35	W	W
36	W	W
37	W	W
38	W	W
39	W	W
40	W	W
41	W	W
42	W	W
43	W	W
44	W	W
45	W	W
46	W	W
47	W	W
48	W	W
49	W	W
50	W	W
51	W	W
52	W	W
53	W	W
54	W	W
55	W	W
56	W	W
57	W	W
58	W	W
59	W	W
60	W	W
61	W	W
62	W	W
63	W	W
64	W	W
65	W	W
66	W	W
67	W	W
68	W	W
69	W	W
70	W	W
71	W	W
72	W	W
73	W	W
74	W	W
75	W	W
76	W	W
77	W	W
78	W	W
79	W	W
80	W	W
81	W	W
82	W	W
83	W	W
84	W	W
85	W	W
86	W	W
87	W	W
88	W	W
89	W	W
90	W	W
91	W	W
92	W	W
93	W	W
94	W	W
95	W	W
96	W	W
97	W	W
98	W	W
99	W	W
100	W	W

Table 6 (continued)

To get actual CPU time savings, numerical experiments were carried out using the test matrix of the type that are encountered in the separation process problems. The test matrices are tabulated in Appendix (D) . The CPU time required for the inversion by partition and by the Gauss-Jordon elemination have been compared for different values of C and presented in Table 1.

The saving in CPU time is becoming increasingly significant as the C increases if the proposed method is employed.

An absorption problem given by Naphthali-Sandholm 3 and another absorption problem given by Holland 1 have been chosen for testing the efficiency of the proposed method. In the first problem, the total number components of the mixture are four and the number stages are twenty. In the other problem the number components are fourteen and stages are eight. The details of the problems are given in Table 2 and 3 and the equilibrium and enthalpy data are given in Appendices B & C. The elements of the Jocabian matrix (the partial derivatives) have been evaluated analytically. The analytical expressions for the derivatives are given in Appendix (A & E).

The two problems have been solved exploiting the sparsity of the submatrices and employing the 'standard' matrix operations. Since no approximations were made while taking of the sparsity in computation, the number of iteration required identical in both the methods. The CPU time required to solve the two problems by these two methods alongwith other details are given in Table 4.

Table 4 shows a substantial reduction in CPU time is achieved in the proposed method. The saving in CPU time becomes increasingly significant as the number of components increases. The proposed method can be employed even interlinked columns.

## CHAPTER 4

CONCLUSIONS

An efficient algorithm for solving the separation processes problems by the well known Naphthali-Sandholm method has been presented. In this algorithm the sparsity the sub-matrices of the Jacobian matrix is exploited in the matrix multiplications and in the inversion of the matrices  $(\bar{\bar{B}}_n - \bar{\bar{A}}_n \bar{\bar{C}}_{n-1}^{-1})$ . It has been shown that the operation count for the proposed algorithm is  $(5C^3 + 14C^2 + 6C)$  compared to  $(2C+1)^3$  with the standard matrix operations. By solving two 'bench-mark' problems, it has been shown that the saving in the CPU time becomes increasingly significant as the number components involved becomes large. In the proposed algorithm, the saving in CPU time in computing the correction vector  $\bar{A} \bar{X}$  is effected, but the number <sup>of</sup> iteration required is the same as with the use of standard matrix operations.

The algorithm can be extended for solving interlinked column employing the method suggested by Hocling and Seader. The computer code need to be tested to determine its effectiveness for distillation of nonideal mixtures, extraction and adsorption problems.

NOMENCLATURE

$A_j$	Submatrices of Jacobian Matrix at the jth row
$B_j$	Submatrices of Jacobian Matrix at the jth row
$C_j$	Submatrices of Jacobian Matrix at the jth row
$C$	Total number of components involved
$L_j$	Overall molar liquid flow rate from jth stage
$V_j$	Overall molar Vapor flow rate from jth stage
$l_{ij}$	Molar liquid flow rate of component i from jth stage
$v_{ij}$	Molar vapor flow rate of component i from jth stage
$K_{ij}$	Distribution coefficient of ith component at jth stage
$\bar{X}$	Vector of variables
$J$	Jacobian matrix
$f_{ij}$	Molar feed rate of the component i into the jth stage
$\bar{F}$	Residual vector
$\bar{F}_j$	Residual vector for the jth stage
$P_j$	P matrix in the Thomas algorithm
$q_j$	External heat input into the jth stage
$h_i$	Molar specific liquid phase enthalpy of component i
$H_i$	Molar specific vapor phase enthalpy of component i
$h_{f_{i,j}}$	Molar specific feed enthalpies of component i
$N$	Total number of stages
$M_{ij}$	Mass balance discrepancy of component i for jth stage

$\Omega_{ij}$	Equilibrium relation discrepancy function for component i at jth stage
$E_j$	Enthalpy balance discrepancy function for the jth stage
$S_j$	Fraction of the vapor stream withdrawn from the jth stage
$s_j$	Fraction of the liquid stream withdrawn from the jth stage

#### Greek letters

$\Delta$	difference in variable
$\eta_j$	murphree efficiency of jth stage
$\delta_{ij}$	Kronecker delta function
$\partial$	partial derivative
$\gamma_i$	activity coefficient of component i
$\lambda$	Thermodynamic parameter
$\alpha$	P matrix of the Thomas Algorithm
$\beta$	q matrix in the Thomas Algorithm

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TABLE 1

CPU time for the inversion of matrix by the proposed method and the Gauss Jordan Elimination

No. of components	CPU time (in Secs.)	Gauss Jordan Elimination (GJ)	Ratio of CPU time (IP/GJ)	Ratio of operation count
Inversion by partition(I.P)				
5	0.14	0.25	0.56	0.76
10	0.59	1.38	0.43	0.70
15	1.96	5.54	0.35	0.68
20	4.99	16.22	0.31	0.66

TABLE 4  
CPU time for two different problems

Problem No.	No. of components	No. of stages	No. of iterations needed	Run No.			CPU in sec.	Ratio of CPU per iteration
				t <sub>1</sub>	t <sub>2</sub>	t <sub>1</sub> + t <sub>2</sub>		
1	4	20	1	7.95	1.95	9.90	0.12	0.12
			2	7.93	1.96	9.89		
			3	7.95	1.96	9.91		
2	14	8	1	784.64	57.12	841.76	0.01	0.01
			2	784.62	57.11	841.73		
			3	784.62	57.14	841.75		

## APPENDIX A

## ELEMENTS OF THE SUBMATRICES

## 1. FOR IDEAL VLE SYSTEM

A. FOR  $\bar{A}$  MATRIX

For  $1 \leq i, j \leq c$  &  $1 \leq n \leq N$

$$\frac{\partial M_{i,n}}{\partial l_{j,n-1}} = \delta_{i,j}, \quad \frac{\partial M_{i,n}}{\partial v_{j,n-1}} = \frac{\partial M_{i,n}}{\partial T_{n-1}} = 0$$

$$\frac{\partial O_{i,n}}{\partial l_{j,n-1}} = \frac{\partial O_{i,n}}{\partial v_{j,n-1}} = \frac{\partial O_{i,n}}{\partial T_{n-1}} = 0$$

$$\frac{\partial E_n}{\partial l_{i,n-1}} = h_{i,n-1}; \quad \frac{\partial E_n}{\partial v_{i,n-1}} = 0$$

$$\frac{\partial E_n}{\partial T_n} = \sum_{j=1}^c l_{i,n-1} \frac{\partial h_{i,n-1}}{\partial T_{n-1}}$$

B. FOR  $\bar{B}$  MATRIX

For  $1 \leq i, j \leq c$  &  $1 \leq n \leq N$

$$\frac{\partial M_{i,n}}{\partial l_{j,n}} = - (1 + s_n) \delta_{ij}$$

$$\frac{\partial M_{i,n}}{\partial v_{j,n}} = - (1 + s_n) \delta_{ij}$$

$$\frac{\partial M_{i,n}}{\partial T_n} = 0$$

Appendix A continued.

$$\frac{\partial o_{i,n}}{\partial l_{j,n}} = \gamma_n k_{i,n} \frac{s_{ij} L_n - l_{in}}{L_n^2}$$

$$\frac{\partial o_{i,n}}{\partial v_{j,n}} = \frac{v_{i,n} - v_n}{v_n^2} s_{ij}$$

$$\frac{\partial o_{i,n}}{\partial T_n} = \gamma_n \frac{l_{i,n}}{L_n} \frac{dk_{i,n}}{dT_n}$$

$$\frac{\partial E_n}{\partial l_{i,n}} = -(1+s_n) h_{i,n}$$

$$\frac{\partial E_n}{\partial v_{i,n}} = -(1+s_n) H_{i,n}$$

$$\frac{\partial E_n}{\partial T_n} = - \sum_{i=1}^c (1+s_n) v_{i,n} \frac{dH_{i,n}}{dT_m} - \sum_{i=1}^c (1+s_n) l_{i,n} \frac{dh_{i,n}}{dT_n}$$

C. FOR  $\bar{C}$  MATRIX

For  $1 \leq i, j \leq c$  &  $1 \leq n \leq N$

$$\frac{\partial M_{i,n}}{\partial l_{j,n+1}} = 0; \quad \frac{\partial M_{i,n}}{\partial v_{j,n+1}} = s_{ij}; \quad \frac{\partial M_{i,n}}{\partial T_{n+1}} = 0$$

$$\frac{\partial o_{i,n}}{\partial l_{j,n+1}} = 0; \quad \frac{\partial o_{i,n}}{\partial v_{j,n+1}} = (1-\gamma_n) \frac{s_{ij} v_{n+1} - v_{i,n+1}}{v_{n+1}^2}$$

## Appendix A continued

$$\frac{\partial \frac{O_{i,n}}{T_{n+1}}}{\partial} = 0 = \frac{\partial E_n}{\partial l_{i,n+1}}$$

$$\frac{\partial E_n}{\partial v_{i,n+1}} = H_{i,n+1} ; \quad \frac{\partial E_n}{\partial T_{n+1}} = \sum_{i=1}^c v_{i,n+1} \frac{dH_{i,n+1}}{dT_{n+1}}$$


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APPENDIX B

## SAMPLE PROBLEM No.1

## DATA

## K values

Material	Temperature	
	100°F	200°F
A	500.0	550.0
B	1.50	1.8
C	0.90	1.00
D	$1.0 \times 10^{-6}$	$1.5 \times 10^{-6}$

Molar liquid enthalpies,  $10^3$  cal/mole.

A	0.01	0.013
B	0.30	0.33
C	0.40	0.44
D	1.50	1.90

Molar vapor enthalpies,  $10^3$  cal/mole

A	1.00	1.002
B	1.80	1.82
C	2.00	2.03
D	5.75	5.95

K values for the temperature range of - 25°F to 40°F and at a pressure of 800 lb/in<sup>2</sup>abs.

Component	$a_{1i}$	$a_{2i}$	$a_{3i}$	$a_{4i}$
CO <sub>2</sub>	- 0.62822223x10 <sup>-1</sup>	0.30688802x10 <sup>-3</sup>	0.39996468x10 <sup>-6</sup>	-0.57899830x10 <sup>-9</sup>
N <sub>2</sub>	0.50596821	-0.43488364x10 <sup>-3</sup>	-0.15009991x10 <sup>-5</sup>	0.34494154x10 <sup>-8</sup>
CH <sub>4</sub>	0.15584934	-0.15205775x10 <sup>-3</sup>	0.50349212x10 <sup>-6</sup>	-0.17713546x10 <sup>-9</sup>
C <sub>2</sub> H <sub>6</sub>	0.91486037x10 <sup>-1</sup>	-0.16355944x10 <sup>-3</sup>	0.33741924x10 <sup>-6</sup>	0.14797150x10 <sup>-9</sup>
C <sub>3</sub> H <sub>8</sub>	0.37769508x10 <sup>-1</sup>	-0.64491702x10 <sup>-4</sup>	0.29233627x10 <sup>-6</sup>	-0.48597680x10 <sup>-11</sup>
i C <sub>4</sub> H <sub>10</sub>	0.36708355x10 <sup>-1</sup>	-0.94310963x10 <sup>-4</sup>	0.28026648x10 <sup>-6</sup>	0.10462797x10 <sup>-10</sup>
n C <sub>4</sub> H <sub>10</sub>	0.37231278x10 <sup>-1</sup>	-0.13635085x10 <sup>-3</sup>	0.37584653x10 <sup>-6</sup>	-0.69237741x10 <sup>-10</sup>
n C <sub>5</sub> H <sub>12</sub>	0.15414596x10 <sup>-1</sup>	-0.34736106x10 <sup>-4</sup>	0.12591028x10 <sup>-6</sup>	0.73157133x10 <sup>-10</sup>
i C <sub>5</sub> H <sub>12</sub>	0.19747034x10 <sup>-1</sup>	-0.40284984x10 <sup>-4</sup>	0.14439195x10 <sup>-6</sup>	0.56656790x10 <sup>-10</sup>
n C <sub>6</sub> H <sub>14</sub>	0.88765752x10 <sup>-3</sup>	0.37082646x10 <sup>-4</sup>	-0.40746951x10 <sup>-7</sup>	0.15187203x10 <sup>-9</sup>
n C <sub>7</sub> H <sub>16</sub>	0.63677356x10 <sup>-2</sup>	-0.64409760x10 <sup>-5</sup>	0.31793974x10 <sup>-7</sup>	0.78284379x10 <sup>-10</sup>
n C <sub>8</sub> H <sub>18</sub>	0.99674799x10 <sup>-2</sup>	-0.34673591x10 <sup>-4</sup>	0.82305291x10 <sup>-7</sup>	0.21022392x10 <sup>-10</sup>
n C <sub>9</sub> H <sub>20</sub>	0.78793392x10 <sup>-2</sup>	-0.23886125x10 <sup>-4</sup>	0.62435951x10 <sup>-7</sup>	0.25793478x10 <sup>-10</sup>
n C <sub>10</sub> H <sub>22</sub>	0.64146556x10 <sup>-2</sup>	-0.16131104x10 <sup>-4</sup>	0.30005250x10 <sup>-7</sup>	0.30266026x10 <sup>-10</sup>

$$K_i = T ( a_{1i} + a_{2i} T + a_{3i} T^2 + a_{4i} T^3 )^3 \quad (T \text{ in } {}^\circ R)$$

Liquid Enthalpies for the Temperature Range of - 25°F to 40°F at P = 800 lb/in<sup>2</sup> abs.

Component	b <sub>1i</sub>	b <sub>2i</sub>	b <sub>3i</sub>	b <sub>4i</sub>
CO <sub>2</sub>	0.22524075x10 <sup>4</sup>	0.5446243x10 <sup>1</sup>	0.2791080x10 <sup>-1</sup>	- 0.18765335x10 <sup>-4</sup>
N <sub>2</sub>	0.15837112x10 <sup>4</sup>	0.3731512x10 <sup>1</sup>	0.17655857x10 <sup>-1</sup>	- 0.14662071x10 <sup>-5</sup>
CH <sub>4</sub>	0.81635181x10 <sup>3</sup>	0.7206460x10 <sup>1</sup>	0.15354034x10 <sup>-1</sup>	- 0.84406456x10 <sup>-5</sup>
C <sub>2</sub> H <sub>6</sub>	0.97404712x10 <sup>3</sup>	0.11454294x10 <sup>2</sup>	0.79399594x10 <sup>-2</sup>	- 0.42183183x10 <sup>-6</sup>
C <sub>3</sub> H <sub>8</sub>	0.21237510x10 <sup>4</sup>	0.46383524x10 <sup>1</sup>	0.31726830x10 <sup>-1</sup>	- 0.12580301x10 <sup>-4</sup>
i C <sub>4</sub> H <sub>10</sub>	0.17543628x10 <sup>4</sup>	0.92456856x10 <sup>1</sup>	0.30206113x10 <sup>-1</sup>	- 0.89584664x10 <sup>-5</sup>
n C <sub>4</sub> H <sub>10</sub>	0.32309192x10 <sup>4</sup>	0.66175545x10 <sup>1</sup>	0.38262386x10 <sup>-1</sup>	- 0.16110935x10 <sup>-4</sup>
i C <sub>5</sub> H <sub>12</sub>	0.33611663x10 <sup>4</sup>	0.39552670x10 <sup>1</sup>	0.54925641x10 <sup>-1</sup>	- 0.25869682x10 <sup>-4</sup>
n C <sub>5</sub> H <sub>12</sub>	0.43454375x10 <sup>4</sup>	0.10596339x10 <sup>2</sup>	0.43731511x10 <sup>-1</sup>	- 0.19637475x10 <sup>-4</sup>
n C <sub>6</sub> H <sub>14</sub>	-0.44150469x10 <sup>4</sup>	0.70354599x10 <sup>2</sup>	-0.67470074x10 <sup>-1</sup>	0.60245657x10 <sup>-4</sup>
n C <sub>7</sub> H <sub>16</sub>	0.66707016x10 <sup>2</sup>	0.18159073x10 <sup>2</sup>	0.38164884x10 <sup>-1</sup>	- 0.42837073x10 <sup>-5</sup>
n C <sub>8</sub> H <sub>18</sub>	-0.10632578x10 <sup>2</sup>	0.19229950x10 <sup>2</sup>	0.40186413x10 <sup>-1</sup>	- 0.70521889x10 <sup>-6</sup>
n C <sub>9</sub> H <sub>20</sub>	-0.79141992x10 <sup>4</sup>	0.81615143x10 <sup>2</sup>	-0.79501927x10 <sup>-1</sup>	0.83943509x10 <sup>-4</sup>
n C <sub>10</sub> H <sub>22</sub>	-0.67810352x10 <sup>4</sup>	0.74108551x10 <sup>2</sup>	-0.58315706x10 <sup>-1</sup>	0.75087155x10 <sup>-4</sup>

$$h_i = b_{1i} + b_{2i}T + b_{3i}T^2 + b_{4i}T^3 \quad (T \text{ in } {}^\circ\text{R}) \text{ Btu/lb mole.}$$

APPENDIX C continued.  
VA FOR ENTHALPIES FOR THE TEMPERATURE RANGE OF - 25°F TO 40°F AT P = 800 lb/in<sup>2</sup> abs.

Component	$c_{1i}$	$c_{2i}$	$c_{3i}$	$c_{4i}$
CO <sub>2</sub>	0.13978977x10 <sup>5</sup>	- 0.96359463x10 <sup>1</sup>	0.38228422x10 <sup>-1</sup>	-0.26870170x10 <sup>-4</sup>
N <sub>2</sub>	0.48638672x10 <sup>4</sup>	- 0.21227379x10 <sup>1</sup>	0.17565668x10 <sup>-1</sup>	-0.11367006x10 <sup>-4</sup>
CH <sub>4</sub>	0.63255430x10 <sup>4</sup>	- 0.20747757x10 <sup>1</sup>	0.18532634x10 <sup>-1</sup>	-0.10630416x10 <sup>-4</sup>
C <sub>2</sub> H <sub>6</sub>	0.10628934x10 <sup>5</sup>	- 0.28718834x10 <sup>1</sup>	0.24877094x10 <sup>-1</sup>	-0.13233222x10 <sup>-4</sup>
C <sub>3</sub> H <sub>8</sub>	0.13954383x10 <sup>5</sup>	- 0.41930256x10 <sup>1</sup>	0.32614145x10 <sup>-1</sup>	-0.15483340x10 <sup>-4</sup>
i C <sub>4</sub> H <sub>10</sub>	0.94088984x10 <sup>4</sup>	0.39262680x10 <sup>2</sup>	-0.55596594x10 <sup>-1</sup>	0.51507392x10 <sup>-4</sup>
n C <sub>4</sub> H <sub>10</sub>	0.57302344x10 <sup>4</sup>	0.75117737x10 <sup>2</sup>	-0.13120884x10 <sup>0</sup>	0.10517908x10 <sup>-3</sup>
i C <sub>5</sub> H <sub>12</sub>	0.83081953x10 <sup>4</sup>	0.75267792x10 <sup>2</sup>	-0.12945843x10 <sup>0</sup>	0.10845697x10 <sup>-3</sup>
n C <sub>5</sub> H <sub>12</sub>	0.12804211x10 <sup>5</sup>	0.61654007x10 <sup>2</sup>	-0.97365201x10 <sup>-1</sup>	0.84398722x10 <sup>-4</sup>
n C <sub>6</sub> H <sub>14</sub>	0.23001684x10 <sup>5</sup>	0.27744919x10 <sup>2</sup>	-0.31545494x10 <sup>-1</sup>	0.49981289x10 <sup>-4</sup>
n C <sub>7</sub> H <sub>16</sub>	0.14876816x10 <sup>5</sup>	0.59342438x10 <sup>2</sup>	-0.81853271x10 <sup>-1</sup>	0.81429855x10 <sup>-4</sup>
n C <sub>8</sub> H <sub>18</sub>	0.32793215x10 <sup>5</sup>	- 0.35040283x10 <sup>2</sup>	0.11162955x10 <sup>0</sup>	-0.42647429x10 <sup>-4</sup>
n C <sub>9</sub> H <sub>20</sub>	0.47024656x10 <sup>5</sup>	- 0.95395035x10 <sup>2</sup>	0.24547529x10 <sup>0</sup>	-0.13209638x10 <sup>-3</sup>
n C <sub>10</sub> H <sub>22</sub>	0.55238211x10 <sup>5</sup>	- 0.13195618x10 <sup>3</sup>	0.32518369x10 <sup>0</sup>	-0.18188384x10 <sup>-3</sup>

$$H_i = c_{1i} + c_{2i} T + c_{3i} T^2 + c_{4i} T^3 \quad (T \text{ in } {}^\circ R) \text{ Btu/1b mole.}$$

APPENDIX D

## Appendix D (continued)

Appendix D (continued)

## APPENDIX E

## ELEMENTS OF MATRICES FOR NONIDEAL SYSTEM

For nonideal system only the following elements need to evaluate from different expressions. Following expressions are evaluated using UNIQUAK model. Because of the lack of time and for model independent programme, this feature was not incorporated.

$$\frac{\partial \sigma_{i,n}}{\partial v_{j,n}} = \frac{\zeta_{ij} v_n - v_{i,n}}{v_n^2} + \frac{l_{i,n}}{L_n} \frac{\sqrt{L}}{(\gamma_{i,n})^2} \frac{\partial \gamma_{i,n}}{\partial v_{j,n}}$$

$$\frac{\partial \sigma_{i,n}}{\partial l_{i,n}} = - \frac{1}{\gamma_{i,n}} \left[ \frac{l_{i,n}}{L_n} \frac{\partial \gamma_{i,n}}{\partial l_{j,n}} + \gamma_{i,n} \left\{ \frac{\zeta_{ij} L_n - l_{i,n}}{L_n^2} \right\} \right]$$

$$\frac{\partial \sigma_{i,n}}{\partial T_n} = - \frac{l_{i,n}}{L_n} \frac{\gamma_{i,n} \frac{\partial \gamma_{i,n}}{\partial T_n} - \gamma_{i,n} \frac{\partial \gamma_{i,n}}{\partial T_n}}{(\gamma_{i,n})^2}$$

$$\gamma_{i,n}^V = \text{Exp} \left[ 1 - \frac{r_i v_n}{\sum_k v_{k,n} r_k} + \ln \left( \frac{r_i v_n}{\sum_j v_{j,n} r_j} \right) \right] \\ - \frac{q_i z}{2} \left\{ 1 - \frac{r_i}{q_i} \frac{\sum_j v_{j,n} q_j}{\sum_j v_{j,n} r_j} + \ln \left( -\frac{r_i}{q_i} \right) \right\} \\ + \ln \left( \frac{\sum_j v_{j,n} q_j}{\sum_j v_{j,n} r_j} \right) + q_i \left\{ 1 - \ln \sum_k \left( \frac{v_{j,n} q_j}{\sum_m v_{m,n} q_m} \right) \right\} \\ - \sum_K \frac{v_{k,n} q_K}{\sum_m v_{m,n} q_m} \Delta_{k,i}$$

Appendix E continued.

Similarly for  $\gamma_{i,n}^L$  where v is substituted by l

$$\begin{aligned} \frac{\partial \gamma_{i,n}^V}{\partial v_{j,n}} &= \gamma_{i,n}^V \left[ - \frac{r_i \sum_k v_{k,n} r_k - v_n r_j}{\left( \sum_k v_{k,n} r_k \right)^2} + \right. \\ &\quad \left. \frac{\sum_k v_{k,n} r_k - r_j v_m}{r_i v_n \left( \sum_k v_{k,n} r_k \right)} - \frac{z}{2} q_i \right] - \frac{r_i}{q_i} \left\{ \frac{\left( \sum_k v_{k,n} r_k \right) q_j \left( \sum_k v_{k,n} q_k \right) r}{\left( \sum_k v_{k,n} r_k \right)^2} \right. \\ &+ \frac{q_j \sum_k (v_{k,n} r_k) - r_j \sum_k w_{k,n} q_k}{\left( \sum_k v_{k,n} q_k \right) \left( \sum_k v_{k,n} r_k \right)} \left. \right\} \\ &- q_i \left\{ \frac{\sum_k (w_{k,n} q_k) \sum_m m_j q_m \Lambda_{j,m} - q_j \sum_m q_m \Lambda_{m,i} w_{m,n}}{\left( \sum_m (v_{m,n} q_m \Lambda_{i,m}) \sum_k (v_{k,n} q_k) \right)} \right. \\ &- \left. q_k \Lambda_{ki} \frac{\sum_{kj} \sum (v_{m,n} q_m \Lambda_{k,m}) - v_{k,n} q_j \Lambda_{k,j}}{\left( \sum_m (v_{m,n} q_m \Lambda_{k,m}) \right)^2} \right\} \\ o_{i,n} &= \frac{v_{i,n}}{V_n} - \frac{l_{i,n}}{L_n} - \frac{\gamma_{i,n}^L}{\gamma_{i,n}^V} \end{aligned}$$

$$\Lambda_{j,i} = \exp(-\frac{a_{ji}}{RT}) \text{ where } a_{ji} \text{ are UNIQUAK parameter.}$$

$$\begin{aligned}
 \frac{\partial \gamma_{i,n}^v}{\partial T_n} &= \gamma_{i,n}^v \left[ - \frac{q_{ii} \sum_j \frac{\partial \Lambda_{i,i}}{\partial T_n}}{\sum_j o_j \Lambda_{i,j}} - \frac{\sum_k \sum_j o_j \Lambda_{k,j} o_k \frac{\partial \Lambda_{k,j}}{\partial T_n}}{\sum_j o_j \Lambda_{i,j}} \right. \\
 &\quad \left. - o_k \Lambda_{k,j} \sum_j o_j \frac{\partial \Lambda_{k,j}}{\partial T_m} \right] \\
 &= - \frac{\gamma_{i,n}^v}{\frac{R T_m^2}{2}} \frac{q_{ii} \sum_j o_j \Lambda_{j,i}}{\sum_j o_j \Lambda_{n,j}} - \\
 &\quad \frac{\sum_k \left( \sum_j o_j \Lambda_{k,j} \right) o_k \Lambda_{k,i}}{\left( \sum_j o_j \Lambda_{i,j} \right)^2} - o_k \Lambda_{k,j} \sum_j o_j \Lambda_{k,i}
 \end{aligned}$$

GENERAL PROGRAM FOR DESIGN AND SIMULATION OF MULTICOMPONENT  
 MULTISTAGE EQUILIBRIUM SEPARATION PROCESSES  
 DEVELOPED AND PROGRAMMED BY L. FIENK  
 EXTENDED NAPHTHALI SANDHOLM METHOD  
 SPARSITY AND SYMMETRY EXPLOITATION  
 LISTING OF SYMBOLS ARE AS FOLLOWS  
 ALJ(J): LIQ. RATE OF THE J TH STAGE  
 V(J): VAP RATE OF THE J TH STAGE  
 SV(J,I): VAP. RATE OF COMPONENT I AT THE J TH STAGE  
 SLJ(J,I): LIQ. RATE OF COMPONENT I AT THE J TH STAGE  
 SQ(J): HEAT INPUT AT THE J TH STAGE  
 SSS(J): FRACTION OF VAP. STREAM TAKEN FROM THE J TH STAGE  
 SSS(J): FRACTION OF LIQ STREAM TAKEN FROM THE J TH STAGE  
 SETA(J): MURPHREE EFFICIENCY OF THE J TH STAGE  
 SH(I): LIQ PHASE ENTHALPY OF COMPONENT I AT ANY STAGE  
 H(I): VAP. PHASE ENTHALPY OF COMPONENT I AT J TH STAGE  
 HF(I): ENTHALPY OF FEED AT ANY STAGE FOR COMPONENT I  
 HH(I): ENTHALPY OF COMPONENT I NEXT BOTTOM STAGE OF THE STAGE  
 TB: TEMPERATURE OF THE VAPOR ENTERING N TH PLATE  
 TO: TEMPERATURE OF THE LIQUID ENTERING INTO FIRST PLATE  
 SLD(I): LIQ. RATE OF COMPONENT I ENTERING AT FIRST PLATE  
 SV(I): VAPOR FLOW RATE OF COMPONENT I ENTERING INTO N TH PLATE  
 VB: TOTAL VAPOR RATE ENTERING INTO THE N TH PLATE  
 UNDER CONSIDERATION  
 SH(I): ENTHALPY OF COMPONENT I NEXT UP STAGE OF THE STAGE  
 UNDER CONSIDERATION  
 AK(I): EQUILIBRIUM CONSTANT VALUE FOR COMPONENT I AT ANY STAGE  
 N: NUMBER OF STAGES  
 C: TOTAL NUMBER OF COMPONENTS INVOLVED FOR SEPARATION  
 SF(J,I): FEED RATE OF COMPONENT I AT THE J TH STAGE  
 TF(J): FEED TEMPERATURE OF THE J TH STAGE  
 Q: ENTHALPY BALANCE NORMALISATION FACTOR

SUBROUTINE ENL : COMPUTES LIQUID PHASE ENTHALPY OF ALL  
 COMPONENTS FOR A GIVEN STAGE  
 SUBROUTINE ENV : COMPUTES VAPOR PHASE ENTHALPY OF ALL  
 COMPONENTS AT A GIVEN STAGE  
 ..... DIST : COMPUTES THE EQUILIBRIUM CONSTANT FOR ALL  
 COMPONENTS AT GIVEN STAGE  
 ..... DDIST : COMPUTES THE DERIVATIVE OF EQUILIBRIUM  
 CONSTANT K w. RLT. TEMPERATURE FOR A STAGE  
 ..... DENL : COMPUTES THE DERIVATIVE OF THE LIQUID  
 PHASE ENTHALPY OF ALL COMPONENTS FOR A  
 PARTICULAR STAGE  
 ..... DENV : COMPUTES THE DERIVATIVE OF THE VAPOR PHASE  
 ENTHALPY OF ALL COMPONENTS FOR A PARTICULAR  
 STAGE  
 ..... BI : COMPUTES THE INVERSION OF B SUBMATRIX  
 ..... B1I : COMPUTE INVERSION OF B1 MATRIX  
 NEW VECTORS

INTEGER C, CT  
 COMMON C, CT, N  
 COMMON /AREA1/SLO, SVB, TB, TO, VB/AREA2/SS, SSS, TF, ETA, SQ  
 COMMON /A1/SA/A2/SC/A3/SE  
 DIMENSION B(29,29), C1(29,29), PBC(14), PC(14), C2(8,29,29)

```

1, F(29), F1(8, 29), A(29, 29), SVB(14), SA(14, 4), SE(14, 4)
2, SL(8, 14), SV(8, 14), AL(8), V(8), SS(8), SSS(8),
3, SF(8, 14), SH(14), H(14), SO(8), SHH(14), HF(14), TF(8),
4, ETA(8), AK(14), R(8), HH(14), PA(14), SLO(14),
5, VOL(20), SC(14, 4)

OPEN (UNIT=21, FILE='S.DAT')

INPUT TERMS MAINLY GUESS VECTOR AND DATA SPECIFICATION.

READ(41, *) N, CT, C
READ(41, *) ((SL(J, I), I=1, C), J=1, N)
READ(41, *) ((SV(J, I), I=1, C), J=1, N)
READ(41, *) ((V(J), J=1, N))
READ(41, *) ((AL(J), J=1, N))
READ(41, *) ((C(J), J=1, N))
READ(41, *) ((TF(J), J=1, N))
READ(41, *) ((SO(J), J=1, N))
READ(41, *) ((ETA(J), J=1, N))
READ(41, *) ((SS(J), J=1, N))
READ(41, *) ((SSS(J), J=1, N))
READ(41, *) R, O, EPS
READ(41, *) ((SF(J, I), I=1, C), J=1, N)
READ(41, *) ((SLO(I), I=1, C))
READ(41, *) ((SVB(I), I=1, C))

READ(41, *) TB, TO, VB
READ(41, *) ((SA(I, J), J=1, 4), I=1, C)
READ(41, *) ((SC(I, J), J=1, 4), I=1, C)
READ(41, *) ((SE(I, J), J=1, 4), I=1, C)

END OF INPUT SPECIFICATION

AEFEO.
IF(CIN.GE.1) GOTO 701
WRITE(44, 2210)
FORMAT(4X, 'INITIAL GUESS OF FLOW RATES AND TEMPERATURE ARE:')
WRITE(44, 2211)
FORMAT(4X, 'VAPOR PHASE COMPONENT FLOW RATES ARE')
WRITE(44, 2212)
FORMAT(4X, 36, '-')
WRITE(44, 2213)
FORMAT(4X, 'COMPONENT NO.', 10X, 'STAGE NOS. ARE')
WRITE(44, 4415)
FORMAT(4X, 13, '-', 10X, 14, '-', /)
WRITE(44, 2214)
FORMAT(20X, 1, '1', 12X, '2', 12X, '3', 12X, '4', 12X, '5', 12X, '6', 12X,
1, '7', 12X, '8', '-')
WRITE(44, 2241)
FORMAT(4X, 116, '-')
WRITE(44, 4451)
FORMAT(/, /)
WRITE(44, 332)(I, (SV(J, I), J=1, N), I=1, C)
FORMAT(4X, I3, 7X, 8(E10.4, 3X)), /)
WRITE(44, 1219)
FORMAT(4X, 'LIQ. COMP. FLOW RATES ARE')
WRITE(44, 2212)
WRITE(44, 2213)
WRITE(44, 4415)
WRITE(44, 2214)
WRITE(44, 2241)

```

```

WRITE(44,332)(I,(SL(J,I),J=1,N),I=1,CD
WRITE(44,4440)
FORMAT(//,*INITIAL VAPOR AND LIQUID RATE AND TEMPERATURE GUESS
1 ARE ,//)
WRITE(44,4467)
WRITE(44,4468)
WRITE(44,7979)
WRITE(44,13)(J,V(J),AL(J),T(J),J=1,N)
WRITE(44,6100)
FORMAT(//,20X,'COMPONENT ',6X,'TOP LIQ.FEED',10X,'BOTTOM VAP.FEED')
1D.)
WRITE(44,6101)
FORMAT(20X,10C('-'),4X,18(' -'),4X,18(' -'))
WRITE(44,6102)(I,SLO(I),SVB(I),I=1,C)
FORMAT((24X,I3+7X,2(E10,0,4X))//)
FORMAT(27X,'IIT KANPUR INDIA')
FORMAT(27X,'1984')
WRITE(5,8)
WRITE(5,14)
WRITE(5,15)
FORMAT(/,4X,'DEVELOPED AND PROGRAMMED BY L. FIENK')
#####
##### COMPUTATION OF AUGMENTED ERROR FUNCTION AT THE GUESS VECTOR
#####
##### # # CONTRIBUTION DUE TO MASS BALANCE # # #
#####
#####
##### EVALUATION OF LD(I) & V(N+1,I) FOR TOTAL CONDENSER
##### TOTAL REBOILER
#####
##### O11.*O
END OF CONDENSER & REBOILER PART
IF ENTERING LIQ. AT PLATE 1 IS NOT AT T(1) ADJUST THIS TL
ACCORDINGLY
TL=F(1)
DO 1 J=1,N-1
P1=1.+SS(J)
P2=1.+SSS(J)
IF(J.NE.1) GOTO 78
DO 1 I=1,C
F1(1,I)=-(SLO(I)+SV(J+1,I)+SF(J,I)-P1*SV(J,I)-P2*SL(J,I))
AEF=AEF+F1(1,I)*F1(1,I)
CONTINUE
GOTO 1
DO 105 I=1,C
F1(J,I)=-(SL(J-1,I)+SV(J+1,I)+SF(J,I)-P1*SV(J,I)-P2*SL(J,I))
AEF=AEF+F1(J,I)*F1(J,I)
CONTINUE
CONTINUE
DO 405 I=1,C
F1(N,I)=-(SL(N-1,I)+SVB(I)+SF(N,I)-P1*SV(N,I)-P2*SL(N,I))
AEF=AEF+F1(N,I)*F1(N,I)
CONTINUE
WRITE(44,18)AEF
FORMAT(//,4X,'AEF AFTER MASS BALANCE',E11.4)
#####
##### END OF EVALUATION OF MASS BALANCE CONTRIBUTION
#####
##### START OF EVALUATION OF THE CONTRIBITION DUE TO
##### ENTHALPY BALNACE
#####

```

```

=====
2 J=1,N-1
TF(J)
P1=1.+SS(J)
P2=1.+SSS(J)
TFF(J)
CALL(J,ENL(TT,SH)
CALL(J,ENV(TT,H))
CALL(J,TFF,SH)
T2=J+1
CALL(J,ENV(T2,HH)
IF(J,NE,1) GOTO 601
DO 23 I=1,C
E=E+SLOC(I)*SHH(I)+SV(2,I)*HH(I)+SF(1,I)*HF(I)
P2*SL(1,I)*SH(I)-P2*SV(1,I)*H(I)
SHH(I)=SH(I)
SH(I)=HH(I)
CONTINUE
F1(1,CT)=(E+SO(1))
AEF=AEE+F1(1,CT)*F1(1,CT)
F1(1,CT)=O*F1(1,CT)
FORMAT(4X,J=1,I3,4X,'AEFOF ENTHALPY =',E11.4)
GO TO 1112
=====
172 I=1,C
E=SL(J-1,I)*SHH(I)+SV(J+1,I)*HH(I)+SF(J,I)*HF(I)
P2*SL(J,I)*SH(I)-P1*SV(J,I)*H(I)
SHH(I)=SH(I)
SH(I)=HH(I)
CONTINUE
F1(J,CT)=(E+SO(J))
AEF=AEE+F1(J,CT)*F1(J,CT)
F1(J,CT)=O*F1(J,CT)
WRITE(5,22)J,AEF
CONTINUE
TF(N)
CALL(ENL(TT,SH)
CALL(ENL(TFF,SH)
CALL(ENV(TB,HH)
=====
272 I=1,C
E=SL(N-1,I)*SHH(I)+SVB(I)*HH(I)+SF(N,I)*HF(I)-P2*SL(N,1)*SH(I)
P1*SV(N,I)*H(I)
CONTINUE
F1(N,CT)=(E+SO(N))
AEF=AEE+F1(N,CT)*F1(N,CT)
F1(N,CT)=O*F1(N,CT)
WRITE(44,22)N,AEF
WRITE(5,22)N,AEF
FFF=AEF
=====

* TO COMPUTE THE LIQUID & VAPOR FLOW RATE FOR ALL STAGES
* CONTRIBUTION DUE TO EQUILIBRIUM CONDITION CONSIDERING
* EFFICIENCY OF ALL STAGES
* =====

```

```

=====
DO 4 J=1,N-1
TT=T(J)
CALL DIST(TT,AK)
DO 4 I=1,C
F1(J,C+I)=-ETA(J)*AK(I)*SL(J,I)/AL(J)-SV(J,I)/V(J)+(1-ETA(J))*  

1SV(J+1,I)/V(J+1)
AEF=AEE+F1(J,C+I)*F1(J,C+I)
CONTINUE
TT=T(N)
CALL DIST(TT,AK)
DO 404 I=1,C
F1(N,C+I)=-ETA(N)*AK(I)*SL(N,I)/AL(N)-SV(N,I)/V(N)+(1,-ETA(N))*  

1SVB(I)/VB
AEF=AEE+F1(N,C+I)*F1(N,C+I)
CONTINUE
=====
# END OF ERROR FUNCTION EVALUATION
=====
IF(FFF-EPS) 5,5,6
=====
FIND THE DIRECTION OF THE N TH PLATE
IT=T(1)
P1=1.+SS(1)
P2=1.+SSS(1)
CALL DIST(TT,AK)
CALL ENL(TT,SH)
CALL ENV(TT,H)
CALL DDIST(TT,PA)
DO 36 I=1,C
B(C+I,2*C+1)=PA(I)
CONTINUE
CALL DENL(TT,PA)
DO 38 I=1,C
B(I,I)=PA(I)
CONTINUE
CALL DENV(TT,PA)
DO 40 I=1,C
B(I,I+C)=PA(I)
CONTINUE
P3=1./AL(1)
TT=0.
BCCT,CT)=0.
AAL=P3*2
VV=1./V(1)^2
DO 41 I=1,C
B(I+1,C+1)=ETA(1)*B(C+I,2*C+1)*P3*SL(1,I)
B(C+1,I)=-P2*SH(I)*0
B(C+1,I+C)=-P1*H(I)*0
B(C+1,2*C+1)=-SV(1,I)*B(I,C+I)+B(2*C+1,2*C+1)
TT=TT-SL(1,I)*B(I,I)
CONTINUE
DO 81 I=1,C
DO 81 IJ=1,C
IF(I.EQ.IJ) GOTO 82
B(I+C,IJ)=-ETA(1)*AK(I)*SL(1,I)*AAL
B(I+C,IJ+C)=SV(1,I)*VV
GOTO 81
8(C+I,IJ)=ETA(1)*AK(I)*(AL(1)-SL(1,I))*AAL
B(C+I,IJ+C)=-(V(1)-SV(1,I))*VV
CONTINUE

```

```

B(2*C+1, 2*C+1)=B(2*C+1, 2*C+1)*P1+TT*P2
B(CT, CT)=B(CT, CT)*0
DO 42 I=1, C
B(I, I) = -P2
B(I, C+I) = -P1
CONTINUE
END OF COMPUTATION OF B1
WRITE(5, 44)((B(I, J), J=1, 2*C+1), I=1, 2*C+1)
FORMAT(//, 4X, 'ELEMENTS OF B MATRIX', /(4X, 9(E11.4, 3X)))
CALL GBI(B)
WRITE(5, 44)((B(I, J), J=1, 2*C+1), I=1, 2*C+1)
COMPUTATION OF C
TT=T(2)
CALL DENV(TT, PA)
CALL ENV(TT, AH)
P3=1/V(2)^2
C1(CT, CT)=0
DO 112 I=1, C
C1(CT, C+I)=HH(I)*0
C1(CT, CT)=C1(CT, CT)+SV(2, I)*PA(I)
C1(CT, C+I)=1.
CONTINUE
DO 83 I=1, C
DO 83 II=1, C
IF(I.EQ.II)GOTO84
C1(I+C, II+C)=(1-ETA(1))*SV(2, I)*P3
GOTO83
C1(I+C, II+C)=(1-ETA(1))*(V(2)-SV(2, I))*P3
CONTINUE
C1(CT, CT)=C1(CT, CT)*0
WRITE(5, 301)((C1(I, J), J=1, CT), I=1, CT)
FORMAT(//, 2X, 'ELEMENTS OF C MATRIX', /(4X, 9(E11.4, 3X)))
WRITE(5, 44)((B(I, J), J=1, CT), I=1, CT)
CALL BCMUL(B, C1)
DO 111 I=1, CT
F(I)=F1(1, I)
DO 111 II=1, CT
C2(1, I, II)=C1(I, II)
CONTINUE
WRITE(5, 301)((C1(I, J), J=1, CT), I=1, CT)
WRITE(5, 305)(F(I), I=1, CT)
FORMAT(//, 2X, 'ELEMENTS OF ERROR VECTOR', /(4X, 9(E13.6, 3X)))
CALL MTMUL1(B, F)
DO 110 I=1, CT
F1(1, I)=F(I)
CONTINUE
WRITE(5, 305)(F(I), I=1, CT)

```

START OF 2ND AND ONWARD STAGES

```

DO 54 J=2, N
P1=1.+SS(J)
P2=1.+SSS(J)
TT=T(J-1)
CALL DENL(TT, H)
AA=0.
CALL ENL(TT, SHH)
DO 55 I=1, C
AA=AA+SL(J-1, I)*H(I)
A(CT, I)=SHH(I)*0
A(I, I)=1.
CONTINUE

```

```

ACCT(CT)=AA*0
END OF COMPUTATION OF ELEMENTS OF A1 MATRIX
WRITE(5,307) ((AC(I,JI),IJ=1,CT),I=1,CT)
FORMAT(//,4X,ELEMENTS OF A MATRIX,/(4X,9(E11.4,3X)))
CALL ACMUL(A,C1)
WRITE(5,301)((C1(I,JI),JI=1,CT),I=1,CT)
CALL AFMUL(A,F)
WRITE(5,305)(F(I),I=1,CT)
P3=1./AL(J)
TT=T(J)
DO 201 I=1,CT
DO 201 II=1,CT
B(I,II)=0.
CONTINUE
CALL DIST(TT,AK)
CALL ENL(TT,SH)
CALL ENV(TT,H)
CALL ODIST(TT,PA)
DO 60 I=1,C
B(C+I,CT)=PA(I)
CONTINUE
CALL DENV(TT,PA)
DO 61 I=1,C
B(I,C+I)=PA(I)
CONTINUE
CALL DENL(TT,PA)
DO 63 I=1,C
B(I,I)=PA(I)
CONTINUE
AAL=P3^2
VV=1/V(J)^2
TT=0.
BCCT,CT)=0.
DO 57 I=1,C
BC(I+C,CT)=ETA(J)*B(C+I,CT)*P3*SL(J,I)
BC(CT,I)=-P2*SH(I)*0
BC(CT,I+C)=-P1*H(I)*0
BC(XT,CT)=B(CT,CT)-SV(J,I)*B(I,C+I)
TT=TT+SL(J,I)*B(I,I)
CONTINUE
DO 85 I=1,C
DO 85 II=1,C
IF(I.EQ.II) GOTO 86
BC(I+C,II)= -ETA(J)*AK(I)*SL(J,I)*AAL
BC(I+C,II+C)=SV(J,I)*VV
GOTO 85
BC(X+I,II)=ETA(J)*AK(I)*(AL(J)-SL(J,I))*AAL
BC(X+I,II+C)=-(V(J)-SV(J,I))*VV
CONTINUE
BCCT,CT)=B(CT,CT)*P1+TT*P2
BCCT,CT)=B(CT,CT)*Q
DO 58 I=1,C
BC(I,I)=-P2
BC(I,C+I)=-P1
CONTINUE
WRITE(5,44)((B(I,JI),JI=1,CT),I=1,CT)
CALL SUBMAT(B,C1)
WRITE(5,44)((B(I,JI),JI=1,CT),I=1,CT)
CALL GB1(B)
WRITE(5,44)((B(I,JI),JI=1,CT),I=1,CT)
DO 160 I=1,CT

```

```

DO 150 III=1,CT
A(I,II)=0
C1(I,II)=0.
CONTINUE
IF(J.EQ.N) GOTO 70
TT=T(J+1)
CALL ENV(TT,HH)
P3=1/V(J+1)^2
THESE A ELEMENTS ARE LEMENTS OF C1 SUBMATRIX
DO 56 I=1,C
C1(CT,C+I)=HH(I)*Q
CONTINUE
CALL DENV(TT,PA)
DO 59 I=1,C
AC(CT,CT)=SV(J+1,I)*PA(I)+A(CT,CT)
C1(I,I+C)=1.
CONTINUE
C1(CT,CT)=Q*A(CT,CT)
DO 87 III=1,C
IF(I.EQ.III) GOTO 88
C1(I+C,III+C)=(1.-ETA(J))*SV(J,I)*P3
C1(I+C,III+C)=(1.-ETA(J))*(V(J+1)-SV(J+1,I))*P3
CONTINUE
WRITE(5,301)((C1(I,JI),JI=1,CT),I=1,CT)
CALL BCMUL(B,C1)
DO 67 III=1,CT
DO 67 III=1,CT
C2(J,III,II)=C1(III,II)
CONTINUE
WRITE(5,301)((C1(I,JI),JI=1,CT),I=1,CT)
DO 69 I=1,CT
F(I)=F1(J,I)-F(I)
CONTINUE
WRITE(5,305)(F(I),I=1,CT)
TYPE*,((B(IJ,IJ),IJ=1,CT),II=1,CT)
FORMAT(4X,'F VALUES ARE:',)
CALL MTMUL1(B,F)
WRITE(5,305)(F(I),I=1,CT)
DO 71 I=1,CT
F1(J,I)=F(I)
DO 71 III=1,CT
AC(I,II)=0.
CONTINUE
CONTINUE
DO 72 JJ=1,N-1
JEN-JJ
DO 75 I=1,CT
F(I)=F1(J+1,I)
DO 75 III=1,CT
C1(I,II)=C2(J,I,II)
CONTINUE
WRITE(38,301)((C1(I,JD),JD=1,CT),I=1,CT)
WRITE(38,305)(F(I),I=1,CT)
CALL CFMUL(C1,F)
WRITE(5,305)(F(I),I=1,CT)
DO 76 I=1,CT
F1(J,I)=-F(I)+F1(J,I)
CONTINUE
CONTINUE
EFF=AEEF

```

```

DF=-1.
DO 135 J=1,N
DO 136 I=1,C
SL(J,I)=SL(J,I)-DF*F1(J,I)
SV(J,I)=SV(J,I)-DF*F1(J,I+C)
CONTINUE
T(J)=T(J)-DF*F1(J,CT)
CONTINUE
IN=IN+1
WRITE(44,200)IN
FORMAT(/,'ITERATION NUMBER=',I3)
AEF=0.
DO 25 J=1,N
V(J)=0.
AL(J)=0.
CONTINUE
DO 202 I=1,CT
DO 202 II=1,CT
B(I,II)=0.
C(I,II)=0.
CONTINUE
DO 371 J=1,N
DO 371 I=1,C
V(J)=V(J)+SV(J,I)
AL(J)=AL(J)+SL(J,I)
CONTINUE
DO 444 J=1,N
CONTINUE
GO TO 16
WRITE(44,9)
FORMAT(/,'SUCCESSFUL CONVERGENT')
WRITE(44,20)IN
FORMAT(/,'ITERATION NUMBER=',I3)
WRITE(44,2410)
FORMAT(4X,'FINAL VALUES OF FLOW RATES AND TEMPERATURE ARE:')
WRITE(44,2411)
FORMAT(4X,'VAPOR PHASE COMPONENT FLOW RATES ARE')
WRITE(44,2412)
FORMAT(4X,'36(-)')
WRITE(44,2413)
FORMAT(4X,'COMPONENT NO.',10X,'STAGE NOS. ARE')
WRITE(44,4315)
FORMAT(4X,'13(-'),10X,14(')'),/)
WRITE(44,2414)
FORMAT(20X,'1',12X,'2',12X,'3',12X,'4',12X,'5',12X,'6',12X,
'7',12X,'8')
WRITE(44,2441)
FORMAT(4X,116('=-'))
WRITE(44,4351)
FORMAT(/)
WRITE(44,392)(I,(SV(J,I),J=1,N),I=1,CD)
FORMAT(4X,I3,7X,BCE10.4,3X),/))
WRITE(44,1319)
FORMAT(/,4X,'LIQ. COMP. FLOW RATES ARE')
WRITE(44,2412)
WRITE(44,2413)
WRITE(44,4315)
WRITE(44,2414)
WRITE(44,2441)
WRITE(44,392)(I,(SL(J,I),J=1,N),I=4,CD)
WRITE(44,4449)

```

```

9 FORMAT(//,4X,'VAPOR AND LIQUID RATE AND TEMPERATURE ARE',//)
1 WRITE(44,4467)
2 FORMAT(4X,42(' '))
3 WRITE(44,4468)
4 FORMAT(4X,'STAGE NUMBER',4X,' VAPOR RATE ',4X,' LIQUID
5 RATE      4X,      TEMPERATURE')
6 WRITE(44,7979)
7 FORMAT(4X,12(' '),4X,19(' '),4X,17(' '),4X,19(' '),/)
8 WRITE(44,13)(J,V(J),AL(J),T(J),J=1,N)
9 FORMAT(8X,I3,5X,E19.8,4X,E17.8,4X,E19.8)
IFAIL=1
STOP
END
SUBROUTINE MTMUL2(A,B)
INTEGER C,CT
COMMON C,CT,N
DIMENSION A(CT,CT),B(CT,CT),D(29,29)
DO 1 I=1,CT
DO 1 J=1,CT
DO 1 IJ=1,CT
D(I,J)=D(I,J)+A(I,IJ)*B(IJ,J)
CONTINUE
DO 2 I=1,CT
DO 2 J=1,CT
B(I,J)=D(I,J)
DO 2 IJ=1,CT
CONTINUE
RETURN
END
SUBROUTINE MTMUL1(A,B)
INTEGER C,CT
COMMON C,CT,N
DIMENSION A(CT,CT),B(CT),D(29)
DO 1 I=1,CT
DO 1 II=1,CT
D(I)=A(I,II)*B(II)+D(I)
CONTINUE
DO 2 I=1,CT
B(I)=D(I)
DO 2 IJ=1,CT
CONTINUE
RETURN
END
SUBROUTINE ENL(T,EL)
INTEGER C,CT
COMMON C,CT,N
COMMON /A2/SC
DIMENSION EL(C),SC(14,4)
DO 1 I=1,C
EL(I)=SC(I,1)+SC(I,2)*T+SC(I,3)*T**2+SC(I,4)*T**3
CONTINUE
RETURN
END
SUBROUTINE DENL(T,EL)
INTEGER C,CT
COMMON C,CT,N
COMMON /A2/SC
DIMENSION EL(C),SC(14,4)
DO 1 I=1,C
EL(I)=SC(I,2)+2.*SC(I,3)*T+3.*SC(I,4)*T**2
CONTINUE

```

```

RETURN
END
SUBROUTINE ENV(T, EV)
INTEGER C, CT
COMMON C, CT, N
COMMON /A3/ SE
DIMENSION EV(C), SE(14,4)
DO 1 I=1, C
EV(I)=SE(I,1)+SE(I,2)*T+SE(I,3)*T^2+SE(I,4)*T^3
CONTINUE
RETURN
END
SUBROUTINE DENV(T, EV)
INTEGER C, CT
COMMON C, CT, N
COMMON /A3/ SE
DIMENSION EV(C), SE(14,4)
DO 1 I=1, C
EV(I)=SE(I,2)+SE(I,3)*2.*T+3.*SE(I,4)*T^2
CONTINUE
RETURN
END
SUBROUTINE SUBMAT(B, CM)
INTEGER C, CT
COMMON C, CT, N
DIMENSION B(CT, CT), C1(CT, CT)
DO 1 I=1, CT
DO 1 J=1, CT
B(I, J)=B(I, J)-C1(I, J)
CONTINUE
RETURN
END
SUBROUTINE DIST(T, AK)
INTEGER C, CT
COMMON C, CT, N
COMMON /A1/ SA
DIMENSION AK(C), SA(14,4)
DO 1 I=1, C
AK(I)=T*(SA(I,1)+SA(I,2)*T+SA(I,3)*T^2+SA(I,4)*T^3)^3
CONTINUE
RETURN
END
SUBROUTINE DDIST(T, AK)
INTEGER C, CT
COMMON C, CT, N
COMMON /A1/ SA
DIMENSION AK(C), SA(14,4)
DO 1 I=1, C
AK(I)=(SA(I,1)+SA(I,2)*T+SA(I,3)*T^2+SA(I,4)*T^3)^3+3.*T*(  

1*SA(I,2)+2.*SA(I,3)*T+3.*SA(I,4)*T^2)*(SA(I,1)+SA(I,2)*T^  

2+SA(I,3)*T^2+SA(I,4)*T^3)^2
CONTINUE
RETURN
END
INVERSION OF GENERAL B MATRIX WITH SPARCITY EXPLOITATION
SUBROUTINE GBI(B)
INTEGER C, CT
COMMON C, CT, N
DIMENSION B(CT, CT), BS(14,14), BS1(14,14), PA(14), PB(14)
DO 1 I=1, C
PA(I)=1./B(I, I)

```

```

CONTINUE
DO 2 I=1,C
DO 2 J=1,C
BS(I,J)=PA(I)*B(I,J+CD)
CONTINUE
DO 3 I=1,C
DO 3 J=1,C
DO 3 IJ=1,C
BS1(I,J)=BS1(I,J)+B(I+C,IJ)*BS(IJ,J)
CONTINUE
DO 4 I=1,C
DO 4 J=1,C
BS1(I,J)=B(I+C,J+C)-BS1(I,J)
CONTINUE
CALL FMI(BS1)
DO 5 I=1,C
DO 5 J=1,C
B(I+C,J+C)=BS1(I,J)
BS1(I,J)=B(I+C,J)*PA(J)
B(I,J+C)=0.
B(I+C,J)=0.
CONTINUE
DO 6 I=1,C
DO 6 J=1,C
BS(I,J)=0.
DO 6 IJ=1,C
B(I,J+C)=B(I,J+C)-BS(I,IJ)*B(IJ+C,J+CD)
CONTINUE
DO 7 I=1,C
DO 7 J=1,C
BS(I,J)=0.
DO 7 IJ=1,C
B(I+C,J)=B(I+C,J)-B(I+C,C+IJ)*BS1(IJ,J)
B(I,J)=B(I,J)-B(I,IJ+C)*BS1(IJ,J)
CONTINUE
DO 9 I=1,C
BS(I,I)=PA(I)
PA(I)=0
DO 9 J=1,C
B(I,J)=B(I,J)+BS(I,J)
CONTINUE
DO 10 I=1,C
DO 10 II=1,C
PA(I)=PA(I)+B(I,II)*B(II,CT)+B(I,II+C)*B(II+C,CT)
PB(I)=PB(I)+B(I+C,II)*B(II,CT)+B(I+C,II+C)*B(II+C,CT)
CONTINUE
DO 11 I=1,C
BB=BB+B(CT,I)*PA(I)+B(CM,I+C)*PB(I)
CONTINUE
B(CT,CT)=1.0/(B(CT,CT)-BB)
DO 12 I=1,C
B(I,CT)=-PA(I)*B(CT,CT)
B(I+C,CT)=-PB(I)*B(CT,CT)
PA(I)=0.
PB(I)=0.
CONTINUE
DO 13 J=1,C
DO 13 II=1,C
PA(J)=PA(J)+B(CT,II)*B(II,J)+B(CT,II+CD)*B(II+C,J)
PB(J)=PB(J)+B(CT,II)*B(II,J+C)+B(CT,II+CD)*B(II+C,J+CD)
CONTINUE

```

```

DO 14 I=1,C
BC(CT,I)=-B(CT,CT)*PA(I)
BC(CT,I+C)=-B(CT,CT)*PB(I)
CONTINUE
DO 15 I=1,C
DO 15 J=1,C
BC(I,J)=B(I,J)-B(I,CT)*PA(J)
BC(I,J+C)=B(I,J+C)-B(I,CT)*PB(J)
BC(I+C,J)=B(I+C,J)-B(I+C,CT)*PA(J)
BC(I+C,J+C)=B(I+C,J+C)-B(I+C,CT)*PB(J)
BS1(I,J)=0.
CONTINUE
BSB=0.
DO 22 I=1,C
PB(I)=0.
CONTINUE
RETURN
END
CORRECTED VERSION OF PRODUCT FORM OF INVERSE
A MATRIX IS TO BE INVERTED
INVERTED MATRIX IS IT AS WELL AS A
SUBROUTINE FMI(A)
INTEGER C, CT
COMMON C, CT
DIMENSION A(C,C), TT(14,14), UI(14,14), T(14,14), ETA(14,14)
DO 1 I=1,C
UI(I,I)=1.
DO 1 J=1,C
TT(I,J)=0.
CONTINUE
DO 5 K=1,C
ETACK(K)=1./A(K,K)
DO 4 I=1,C
IF(I.EQ.K) GOTO 4
ETAC(I,K)=-A(I,K)/A(K,K)
CONTINUE
DO 6 I=1,C
ETAC(I,K)=ETA(I,K)-UI(I,K)
CONTINUE
DO 7 I=1,C
DO 7 J=1,C
T(I,J)=UI(I,J)+ETA(I,K)*UI(K,J)
CONTINUE
DO 8 I=1,C
DO 8 J=1,C
ETAC(I,J)=0.
IF(K.NE.1) GOTO 8
TT(I,J)=T(I,J)
CONTINUE
DO 9 I=1,C
DO 9 J=K,C
DO 9 IJ=1,C
ETAC(I,J)=T(I,IJ)*A(IJ,J)+ETA(I,J)
CONTINUE
DO 10 I=1,C
DO 10 J=1,C
A(I,J)=ETA(I,J)
ETA(I,J)=0.
CONTINUE
IF(K.EQ.1) GOTO 5

```

```

DO 11 I=1,C
DO 11 J=1,C
DO 11 IJ=1,C
ETA(I,J)=T(I,IJ)*TT(IJ,J)+ETA(I,J)
CONTINUE
DO 12 I=1,C
DO 12 J=1,C
TT(I,J)=ETA(I,J)
ETA(I,J)=0.
CONTINUE
DO 14 I=1,C
DO 14 J=1,C
A(I,J)=TT(I,J)
CONTINUE
RETURN
END
INVERSION B1 MATRIX
DURING INVERSION SPARCITY IS EXPLOITED AND COMPUTATIONALLY
FASTER THAN AS USUAL INVERSION
SUBROUTINE B1I(B)
INTEGER C,CT
COMMON C,CT,N
DIMENSION B(CT,CT),SB(14,14),PA(14),PB(14)
DO 1 I=1,C
PA(I)=1./B(I,I)
PB(I)=PA(I)*B(I,I+C)
CONTINUE
DO 2 I=1,C
DO 2 J=1,C
SB(I,J)=B(I+C,J)*PB(J)
SB(I,J)=B(I+C,J+C)-SB(I,J)
CONTINUE
CALL FMI(SB)
DO 3 I=1,C
DO 3 J=1,C
B(I+C,J+C)=SB(I,J)
B(I,J+C)=-PB(I)*SB(I,J)
SB(I,J)=0.
CONTINUE
DO 4 I=1,C
DO 4 J=1,C
B(I+C,J)=-B(I+C,J)*PA(J)
B(I,J)=0.
CONTINUE
DO 16 I=1,C
B(I,I)=PA(I)
DO 16 J=1,C
DO 16 IJ=1,C
SB(I,J)=SB(I,J)+B(I,IJ+C)*B(IJ+C,J)
CONTINUE
DO 17 I=1,C
DO 17 J=1,C
B(I,J)=B(I,J)+SB(I,J)
SB(I,J)=0.
CONTINUE
DO 18 I=1,C
DO 18 J=1,C
DO 18 IJ=1,C
SB(I,J)=SB(I,J)+B(I+C,IJ+C)*B(IJ+C,J)
CONTINUE

```

```

DO 5 I=1,C
PA(I)=0.
PB(I)=0.
DO 5 J=1,C
B(I+C,J)=SB(I,J)
SB(I,J)=0.
CONTINUE
DO 10 I=1,C
DO 10 II=1,C
PA(I)=PA(I)+B(I,II)*B(II,CT)+B(I,II+C)*B(II+C,CT)
PB(I)=PB(I)+B(I+C,II)*B(II,CT)+B(I+C,II+C)*B(II+C,CT)
CONTINUE
DO 11 I=1,C
BB=BB+B(CT,I)*PA(I)+B(CT,I+C)*PB(I)
CONTINUE
B(CT,CT)=1./(B(CT,CT)-BB)
DO 12 I=1,C
B(I,CT)=-PA(I)*B(CT,CT)
B(I+C,CT)=-PB(I)*B(CT,CT)
PA(I)=0.
PB(I)=0.
CONTINUE
DO 13 J=1,C
DO 13 II=1,C
PA(J)=PA(J)+B(CT,II)*B(II,J)+B(CT,II+C)*B(II+C,J)
PB(J)=PB(J)+B(CT,II)*B(II,J+C)+B(CT,II+C)*B(II+C,J+C)
CONTINUE
DO 14 I=1,C
B(CT,I)=-B(CT,CT)*PA(I)
B(CT,I+C)=-B(CT,CT)*PB(I)
CONTINUE
DO 15 I=1,C
DO 15 J=1,C
B(I,J)=B(I,J)-B(I,CT)*PA(J)
B(I,J+C)=B(I,J+C)-B(I,CT)*PB(J)
B(I+C,J)=B(I+C,J)-B(I+C,CT)*PA(J)
B(I+C,J+C)=B(I+C,J+C)-B(I+C,CT)*PB(J)
CONTINUE
BB=0.
RETURN
END

SUBROUTINE ACMUL(A,C1)
INTEGER C, CT
COMMON C, CT, N
DIMENSION A(CT,CT), C1(CT,CT)
DO 1 I=1,C
DO 1 J=1,C+1
C1(I+C,J+C)=0.
CONTINUE
DO 2 I=1,C
DO 2 J=1,C
C1(1,I)=C1(1,I)+A(CT,J)*C1(J,I+C)
CONTINUE
C1(CT,C+1)=C1(1,I)+A(CT,CT)*C1(CT,I+C)
C1(1,I)=0.
AA=A*A+A(CT,I)*C1(I,CT)
CONTINUE
C1(CT,CT)=AA+A(CT,CT)*C1(CT,CT)
AA=0.
RETURN
END

```

```

SUBROUTINE AFMUL(A,F)
INTEGER C,CT
COMMON C,CT,N
DIMENSION A(CT,CT),F(CT)
DO 1 I=1,C
E(C+I)=0
AA=A(CT,I)*F(I)
CONTINUE
E(CT)=AA+F(CT)*A(CT,CT)
AA=0
RETURN
END
SUBROUTINE BCMUL(B,C1)
INTEGER C,CT
COMMON C,CT,N
DIMENSION B(CT,CT),C1(CT,CT)
DO 2 I=1,CT
DO 2 J=1,CT
DO 2 K=1,CT
C1(I,J)=C1(I,J)+B(I,K)*C1(K,J+CD)
CONTINUE
DO 1 I=1,CT
DO 1 J=1,CT
C1(I,J+C)=C1(I,J)
C1(I,J)=0.
CONTINUE
DO 4 I=1,CT
DO 4 K=1,CT
C1(I,1)=C1(I,1)+B(I,K)*C1(K,CT)
CONTINUE
DO 3 I=1,CT
C1(I,CT)=C1(I,1)
C1(I,1)=0.
CONTINUE
RETURN
END
SUBROUTINE CFMUL(C1,F)
INTEGER C,CT
COMMON C,CT,N
DIMENSION C(N,CT,CT),F(CT)
DO 1 I=1,CT
DO 1 K=1,C+1
C1(I,1)=C1(I,1)+C1(I,K+CD)*F(C+K)
CONTINUE
DO 2 I=1,CT
C1(I)=C1(I,1)
C1(I,1)=0.
CONTINUE
RETURN
END

```

## INPUT SPECIFICATION OF PROBLEM NUMBER 1

GENERAL PROGRAM FOR DESIGN AND SIMULATION OF MULTICOMPONENT  
MULTISTAGE EQUILIBRIUM SEPARATION PROCESSES

PROGRAMMED BY L. FIENK

NAPHTHALI SANDHOLM METHOD

LISTING OF SYMBOLS ARE AS FOLLOWS

AL(J): LIQ. RATE OF THE J TH STAGE

VC(J): VAP. RATE OF THE J TH STAGE

SV(J, I): VAP. RATE OF COMPONENT I AT THE J TH STAGE

SLOC(J, I): LIQ. RATE OF COMPONENT I AT THE J TH STAGE

SOC(J, I): HEAT INPUT AT THE J TH STAGE

SSC(J, I): FRACTION OF VAP. STREAM TAKEN FROM THE J TH STAGE

SSS(J, I): FRACTION OF LIQ. STREAM TAKEN FROM THE J TH STAGE

ETA(J, I): MURPHREE EFFICIENCY OF THE J TH STAGE

SH(I): LIQ. PHASE ENTHALPY OF COMPONENT I AT ANY STAGE

H(V): VAP. PHASE ENTHALPY OF COMPONENT I AT J TH STAGE

HFC(I): ENTHALPY OF FEED AT ANY STAGE FOR COMPONENT I

HC(I): ENTHALPY OF COMPONENT I NEXT BOTTOM STAGE OF THE STAGE

TB: TEMPERATURE OF THE VAPOR ENTERING N TH PLATE

TO: TEMPERATURE OF THE LIQUID ENTERING INTO FIRST PLATE

SLOC(I): LIQ. RATE OF COMPONENT I ENTERING AT FIRST PLATE

SVOC(I): VAPOR FLOW RATE OF COMPONENT I ENTERING INTO N TH PLATE

VB: TOTAL VAPOR RATE ENTERING INTO THE N TH PLATE

UNDER CONSIDERATION

SHH(I): ENTHALPY OF COMPONENT I NEXT UP STAGE OF THE STAGE

UNDER CONSIDERATION

AK(I): EQUILIBRIUM CONSTANT VALUE FOR COMPONENT I AT ANY STAGE

N: NUMBER OF STAGES

C: TOTAL NUMBER OF COMPONENTS INVOLVED FOR SEPARATION

SF(J, I): FEED RATE OF COMPONENT I AT THE J TH STAGE

TF(J): FEED TEMPERATURE OF THE J TH STAGE

Q: ENTHALPY BALANCE NORMALISATION FACTOR

SUBROUTINE ENL : COMPUTES LIQUID PHASE ENTHALPY OF ALL  
COMPONENTS FOR A GIVEN STAGE

SUBROUTINE ENV : COMPUTES VAPOR PHASE ENTHALPY OF ALL  
COMPONENTS AT A GIVEN STAGE

..... DIST : COMPUTES THE EQUILIBRIUM CONSTANT FOR ALL  
COMPONENTS AT GIVEN STAGE

..... DDIST : COMPUTES THE DERIVATIVE OF EQUILIBRIUM  
CONSTANT K W.R.T. TEMPERATURE FOR A STAGE

..... DENL : COMPUTES THE DERIVATIVE OF THE LIQUID  
PHASE ENTHALPY OF ALL COMPONENTS FOR A  
PARTICULAR STAGE

..... DENV : COMPUTES THE DERIVATIVE OF THE VAPOR PHASE  
ENTHALPY OF ALL COMPONENTS FOR A PARTICULAR  
STAGE

..... BI : COMPUTES THE INVERSION OF B SUBMATRIX

..... BII : COMPUTE INVERSION OF B1 MATRIX  
NEW VECTORS

INTEGER C, CT

COMMON C, CT, N

COMMON /AREA1/SLO, SVB, TB, TO, VB/AREA2/SS, SSS, TF, ETA, SQ

COMMON /A1/SA/A2/SC/A3/SE

DIMENSION B(29,29), C1(29,29), PB(14), PC(14), C2(8,29,29)

```

1, F(29), F1(8,29), A(29,29), SVB(14), SA(14,4), SE(14,4)
2, SL(8,14), SV(8,14), AL(8), V(8), SS(8), SSS(8),
3, SF(8,14), SH(14), H(14), SO(8), SHH(14), HF(14), TF(8),
4, ETA(8), AK(14), T(8), HH(14), PA(14), SLO(14),
5, VD(20), SC(14,4)

OPEN (UNIT=21,FILE='S.DAT')
INPUT TERMS MAINLY GUESS VECTOR AND DATA SPECIFICATION.
READ(41,*), N, CT, C
READ(41,*), (SL(I,J), I=1,C), J=1,N)
READ(41,*), (SV(J,I), I=1,C), J=1,N)
READ(41,*), (V(J), J=1,N)
READ(41,*), (AL(J), J=1,N)
READ(41,*), (TC(J), J=1,N)
READ(41,*), (TF(J), J=1,N)
READ(41,*), (SO(J), J=1,N)
READ(41,*), (ETA(J), J=1,N)
READ(41,*), (SS(J), J=1,N)
READ(41,*), (SSS(J), J=1,N)
READ(41,*), EPS
READ(41,*), (SF(J,I), I=1,C), J=1,N)
READ(41,*), (SLO(I), I=1,C)
READ(41,*), (SVB(I), I=1,C)

READ(41,*), TB, TO, VB
READ(41,*), (SA(I,J), J=1,4), I=1,3D
READ(41,*), (SC(I,J), J=1,4), I=1,3D
READ(41,*), (SE(I,J), J=1,4), I=1,3D
END OF INPUT SPECIFICATION.
AEF=0.
IF(CIN.GE.1) GOTO 701
WRITE(44,2210)
FORMAT(4X,'INITIAL GUESS OF FLOW RATES AND TEMPERATURE ARE:')
WRITE(44,2211)
FORMAT(4X,'VAPOR PHASE COMPONENT FLOW RATES ARE')
WRITE(44,2212)
FORMAT(4X,36(' '))
WRITE(44,2213)
FORMAT(4X,'COMPONENT NO.',10X,'STAGE NOS. ARE')
WRITE(44,4415)
FORMAT(4X,13(' '),10X,14(' ',''),/)
WRITE(44,2214)
FDIMAT(20X,'1',12X,'2',12X,'3',12X,'4',12X,'5',12X,'6',12X,
1'7',12X,'8')
WRITE(44,2241)
FORMAT(4X,116(' '))
WRITE(44,4451)
FORMAT(4X,3322(I,(SV(J,I),J=1,N),I=1,C)
FDIMAT(4X,I3,7X,8(E10.4,3X)),/)
WRITE(44,1219)
FORMAT(4X,'LIQ. COMP. FLOW RATES ARE')
WRITE(44,2212)
WRITE(44,2213)
WRITE(44,4415)
WRITE(44,2214)
WRITE(44,2241)
WRITE(44,3322(I,(SL(J,I),J=1,N),I=1,C)
WRITE(44,4440)

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```

40 FORMAT(//,'INITIAL VAPOR AND LIQUID RATE AND TEMPERATURE GUESS
1 ARE //)
WRITE(44,4467)
WRITE(44,4468)
WRITE(44,7979)
WRITE(44,13)(J,V(J),AL(J),T(J),J=1,N)
WRITE(44,6100)
FORMAT(//,20X,'COMPONENT ',6X,'TOP LIQ.FEED',10X,'BOTTOM VAP.FEE
1D')
WRITE(44,6101)
FORMAT(20X,10(' -'),4X,18(' -'),4X,18(' -'))
WRITE(44,6102)(I,SLO(I),SVB(I),I=1,C)
FORMAT(44X,I3,7X,2(E18.8,4X))/)
FORMAT(27X,'IT KANPUR INDIA ')
FORMAT(27X,'1984')
WRITE(5,8)
WRITE(5,14)
WRITE(5,15)
FORMAT(/,4X,'DEVELOPED AND PROGRAMMED BY L. FIENK')
#####
# COMPUTATION OF AUGMENTED ERROR FUNCTION AT THE GUESS VECTOR
# #####
# # CONTRIBUTION DUE TO MASS BALANCE # #
#####
EVALUATION OF LO(I) & V(N+1,I) FOR TOTAL CONDENSER
& TOTAL REBOILER
#####
Q=1.
Q=1./O
END OF CONDENSER & REBOILER PART
IF ENTERING LIQ. AT PLATE 1 IS NOT AT T(1) ADJUST THIS TO
ACCORDINGLY
TL=T(1)
T(N+1)=T(N)
DO 1 J=1,N-1
P1=1.+SS(J)
P2=1.+SSS(J)
IF(J.NE.1) GOTO 78
DO 1111 I=1,C
F1(1,I)=-(SLO(I)+SV(J+1,I)+SF(J,I)-P1*SV(J,I)-P2*SL(J,I))
AEF=AEF+F1(1,I)*F1(1,I)
FORMAT(4X,'AEF AFTER MASS BALANCE',E11.4)
CONTINUE
GOTO 1
DO 105 I=1,C
F1(J,I)=-(SL(J-1,I)+SV(J+1,I)+SF(J,I)-P1*SV(J,I)-P2*SL(J,I))
AEF=AEF+F1(J,I)*F1(J,I)
CONTINUE
DO 405 I=1,C
F1(N,I)=-(SL(N-1,I)+SVB(I)+SF(N,I)-P1*SV(N,I)-P2*SL(N,I))
AEF=AEF+F1(N,I)*F1(N,I)
CONTINUE
WRITE(44,18) AEF
#####
# END OF EVALUATION OF MASS BALANCE CONTRIBUTION
# #####
# START OF EVALUATION OF THE CONTRIBUTION DUE TO
# ENTHALPY BALNACE
#####

```

```

E=0
DO 2 J=1,N-1
TT=T(J)
P1=1.+SS(J)
P2=1.+SSS(J)
TFF=TF(J)
CALL ENL(TT,SH)
IF(J.NE.1) GOTO 601
CALL ENV(TT,H)
CALL ENL(TO,SHH)
CALL ENL(TFF,HF)
C2=T(J+1)
CALL ENV(T2,HH)
IF(J.NE.1) GOTO 26
DO 23 I=1,C
E=E+SLOC(I)*SHH(I)+SV(2,I)*HH(I)+SF(1,I)*HF(I)
1-P2*SLC(I)*SH(I)-P1*SV(1,I)*H(I)
SHH(I)=SH(I)
HC(H(I))=HH(I)
CONTINUE
E1(1,CT)=(E+SO(1))
AEF=AEE+F1(1,CT)*F1(1,CT)
F1(1,CT)=Q*F1(1,CT)
FORMAT(4X,J=,I3,4X,'AEFOF ENTHALPY =',E11.4)
GO TO 1112
DSB=0
DO 172 I=1,C
E=E+SL(J-1,I)*SHH(I)+SV(J+1,I)*HH(I)+SF(J,I)*HF(I)
1-P2*SLC(J,I)*SH(I)-P1*SV(J,I)*H(I)
SHH(I)=SH(I)
HC(H(I))=HH(I)
CONTINUE
E1(J,CT)=-(E+SO(J))
AEE=AEE+F1(J,CT)*F1(J,CT)
F1(J,CT)=Q*F1(J,CT)
WRITE(5,22)J,AEE
CONTINUE
CT=T(N)
TFF=TF(N)
CALL ENL(TT,SH)
CALL ENL(TFF,HF)
CALL ENV(TB,HH)
DO 272 I=1,C
E=E+SL(N-1,I)*SHH(I)+SVB(I)*HH(I)+SF(N,I)*HF(I)-P2*SL(N,I)*SH(I)
1-P1*SV(N,I)*H(I)
CONTINUE
F1(N,CT)=-(E+SO(N))
AEE=AEE+F1(N,CT)*F1(N,CT)
F1(N,CT)=Q*F1(N,CT)
FEE=AEE
WRITE(44,22)N,AEE
WRITE(5,22)N,AEE
# TO COMPUTE THE LIQUID & VAPOR FLOW RATE FOR ALL STAGES
# CONTRIBUTION DUE TO EQUILIBRIUM CONDITION CONSIDERING
# EFFICIENCY OF ALL STAGES

```

```

DO 4 J=1,N-1
TT=T(J)
CALL DIST(TT,AK)
DO 4 I=1,C
F1(J,C+I)=-ETA(J)*AK(I)*SL(J,I)/AL(J)-SV(J,I)/V(J)+(1-ETA(J))*  

1 SV(J+1,I)/V(J+1)
AEF=AEF+F1(J,C+I)*F1(J,C+I)
CONTINUE
TT=T(N)
CALL DIST(TT,AK)
DO 404 I=1,C
F1(N,C+I)=-ETA(N)*AK(I)*SL(N,I)/AL(N)-SV(N,I)/V(N)+(1-ETA(N))*  

1 SVB(I)/VB
AEF=AEF+F1(N,C+I)*F1(N,C+I)
CONTINUE
=====
# END OF ERROR FUNCTION EVALUATION
=====
IF(FFF-EPS) 5,5,6
=====
FIND THE DIRECTION OF THE N TH PLATE
TT=T(1)
P1=1.+SS(1)
P2=1.+SSS(1)
CALL DIST(TT,AK)
CALL ENL(TT,SH)
CALL ENV(TT,H)
CALL DDIST(TT,PA)
DO 36 I=1,C
(C+I,2*C+1)=PA(I)
CONTINUE
CALL DENL(TT,PA)
DO 38 I=1,C
(I,I)=PA(I)
CONTINUE
CALL DENV(TT,PA)
DO 40 I=1,C
(I,I+C)=PA(I)
CONTINUE
P3=1./AL(1)
TT=0.
B(CT,CT)=0.
AAL=P3*2
VV=1./V(1)**2
DO 41 I=1,C
B(I+C,2*C+1)=ETA(1)*B(C+I,2*C+1)*P3*SL(1,I)
B(C+2*C+1,I)=-P2*SH(I)*0
B(C+2*C+1,C+I)=-P1*H(I)*0
B(C+2*C+1,2*C+1)=-SV(1,I)*B(I,C+I)+B(2*C+1,2*C+1)
TT=TT-SL(1,I)*B(I,I)
CONTINUE
81 I=1,C
DO 81 IJ=1,C
IF(I.EQ.IJ) GOTO 82
B(I+C,IJ)=-ETA(1)*AK(I)*SL(1,I)*AAL
B(I+C,IJ+C)=SV(1,I)*VV
GOTO 81
(I+C,IJ)=ETA(1)*AK(I)*(AL(1)-SL(1,I))*AAL
(I+C,IJ+C)=-(V(1)-SV(1,I))*VV
CONTINUE
B(2*C+1,2*C+1)=B(2*C+1,2*C+1)*P1+TT*P2

```

```

B(CT, CT)=B(CT, CT)*Q
DO 42 I=1,C
B(I,I)=-P2
B(I,C+1)=-P1
CONTINUE
END OF COMPUTATION OF B1
WRITE(5,44)((B(I,J),J=1,2*C+1),I=1,2*C+1)
FORMAT(//,4X,'ELEMENTS OF B MATRIX',(4X,9(E11.4,3X)))
CALL GBI(B)
WRITE(5,44)((B(I,J),J=1,2*C+1),I=1,2*C+1)
COMPUTATION OF C
TT=T(2)
CALL DENV(TT,PA)
CALL ENV(TT,HH)
P3=1/VC2)^2
C1(CT,CT)=0.0
DO 112 I=1,C
C1(CT,C+I)=HH(I)*0
C1(CT,C+I)=C1(CT,CT)+SV(2,I)*PA(I)
C1(C+I,C+I)=1.
CONTINUE
DO 83 I=1,C
DO 83 II=1,C
IF(I,EO,II)GOTO84
C1(I+C,II+C)=(1-ETA(1))*SV(2,I)*P3
GOTO 83
C1(I+C,II+C)=(1-ETA(1))*(V(2)-SV(2,I))*P3
CONTINUE
C1(CT,CT)=C1(CT,CT)*0
WRITE(5,301)((C1(I,J),J=1,CT),I=1,CT)
FORMAT(//,2X,'ELEMENTS OF C MATRIX',(4X,9(E11.4,3X)))
WRITE(5,44)((B(I,J),J=1,CT),I=1,CT)
CALL MTMUL2(B,C1)
DO 111 I=1,CT
F(I)=F1(1,I)
DO 111 II=1,CT
C2(1,I,II)=C1(I,II)
CONTINUE
WRITE(5,301)((C1(I,J),J=1,CT),I=1,CT)
WRITE(5,305)(F(I),I=1,CT)
FORMAT(//,2X,'ELEMENTS OF ERROR VECTOR',(4X,9(E13.6,3X)))
CALL MTMUL1(B,F)
DO 110 I=1,CT
F1(1,I)=F(I)
CONTINUE
WRITE(5,305)(F(I),I=1,CT)
START OF 2ND AND ONWORD STAGES

DO 54 J=2,N
P1=1.+SS(J)
P2=1.+SSS(J)
TT=T(J-1)
CALL DENL(TT,H)
AA=0.
CALL ENL(TT,SHH)
DO 55 I=1,C
AA=AA+SL(J-1,I)*H(I)
A(CT,I)=SHH(I)*0
A(I,I)=1.
CONTINUE
A(CT,CT)=AA*0

```

```

END OF COMPUTATION OF ELEMENTS OF A MATRIX
WRITE(5,307)((A(I,J),IJ=1,CT),I=1,CT)
FORMAT(//,4X,'ELEMENTS OF A MATRIX',(4X,9(E11.4,3X)))
CALL MTMUL2(A,C1)
WRITE(5,301)((C1(I,J),JI=1,CT),I=1,CT)
CALL MTMUL1(A,F)
WRITE(5,305)(F(I),I=1,CT)
P3=1/AL(J)
TT=T(J)
DO 201 I=1,CT
DO 201 II=1,CT
B(I,II)=0.
CONTINUE
CALL DIST(TT,AK)
CALL ENL(TT,SH)
CALL ENV(TT,H)
CALL DDIST(TT,PA)
DO 60 I=1,C
B(C+I,CT)=PA(I)
CONTINUE
CALL DENV(TT,PA)
DO 61 I=1,C
B(I,C+I)=PA(I)
CONTINUE
CALL DENL(TT,PA)
DO 63 I=1,C
B(I,I)=PA(I)
CONTINUE
AAL=P3*2
VV=1/V(J)**2
TT=0.
B(C+CT,CT)=0.
DO 57 I=1,C
B(C+I,CT)=ETA(J)*B(C+I,CT)*P3*SL(J,I)
B(C+I,I)=-P2*SH(I)*0
B(C+I,C+I)=-P1*H(I)*0
B(C+I,CT)=B(CT,CT)-SV(J,I)*B(I,C+I)
TT=TT-SL(J,I)*B(I,I)
CONTINUE
DO 85 I=1,C
DO 85 II=1,C
IF(I.EQ.II) GOTO 86
B(I+C,II)=-ETA(J)*AK(I)*SL(J,I)*AAL

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85      B(I+C,II+C)=SV(J,I)*VV
86      GOTO 85
87      B(C+I,II)=ETA(J)*AK(I)*(AL(J)-SL(J,I))*AAL
88      B(C+I,II+C)=-(V(J)-SV(J,I))*VV
89      CONTINUE
90      B(CT,CT)=B(CT,CT)*P1+TT*P2
91      B(CT,CT)=B(CT,CT)*Q
92      DO 58 I=1,C
93      B(I,I)=-P2
94      B(I,C+I)=-P1
95      CONTINUE
96      WRITE(5,44)((B(I,JI),JI=1,CT),I=1,CT)
97      CALL SUBMAT(B,C1)
98      WRITE(5,44)((B(I,JI),JI=1,CT),I=1,CT)
99      CALL GB1(B)
100     WRITE(5,44)((B(I,JI),JI=1,CT),I=1,CT)
101     DO 160 I=1,CT
102     DO 160 II=1,CT
103     A(I,II)=0
104     C1(I,II)=0.
105     CONTINUE
106     IF(J.EQ.N) GOTO 70
107     TT=1/(J+1)
108     CALL ENV(TTAHH)
109     P3=1/V(J+1)**2
110     THESE A ELEMENTS ARE ELEMENTS OF C1 SUBMATRIX
111     DO 56 I=1,C
112     DO 1(C1(I,C+I)=HH(I)*Q
113     CONTINUE
114     CALL DENV(TT,PA)
115     DO 59 I=1,C
116     A(CT,CT)=SV(J+1,I)*PA(I)+A(CT,CT)
117     C1(I,C+I)=1.
118     CONTINUE
119     C1(CT,CT)=0*A(CT,CT)
120     DO 87 III=1,C
121     IF(I.EQ.III) GOTO 88
122     C1(I+C,II+C)=(1.-ETA(J))*SV(J,I)*P3
123     C1(I+C,II+C)=(1.-ETA(J))*(V(J+1)-SV(J+1,I))*P3
124     CONTINUE
125     WRITE(5,301)((C1(I,JI),JI=1,CT),I=1,CT)
126     CALL MTMUL2(B,C1)
127     DO 67 III=1,CT
128     DO 67 II=1,CT
129     C2(J,III,II)=C1(III,II)
130     CONTINUE
131     WRITE(5,301)((C1(I,JI),JI=1,CT),I=1,CT)
132     DO 69 I=1,CT
133     F(I)=F1(J,I)-F(I)
134     CONTINUE
135     WRITE(5,305)(F(I),I=1,CT)
136     TYPE*((B(CI,IJ),IJ=1,CT),II=1,CM)
137     CALL MTMUL1(B,F)
138     WRITE(5,305)(F(I),I=1,CT)
139     DO 71 I=1,CT
140     F1(J,I)=F(I)
141     DO 71 II=1,CT
142     A(I,II)=0.
143     CONTINUE
144     CONTINUE

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```

DO 72 JJ=1,N-1
J=N-JJ
DO 75 I=1,CT
F(I)=F1(J+1,I)
DO 75 II=1,CT
C01(I,II)=C2(J,I,II)
CONTINUE
WRITE(38,305)(F(I),I=1,CT)
CALL MTMUL1(C1,F)
WRITE(5,305)(F(I),I=1,CT)
DO 76 I=1,CT
F1(J,I)=-F(I)+F1(J,I)
CONTINUE
CONTINUE
AEF=0
FF=1
DO 135 J=1,N
DO 136 I=1,C
SL(J,I)=SL(J,I)-DF*F1(J,I)
SV(J,I)=SV(J,I)-DF*F1(J,I+C)
CONTINUE
T(J)=T(J)-DF*F1(J,CT)
CONTINUE
IN=IN+1
WRITE(44,200)IN
FORMAT(/,ITERATION NUMBER=',I30)
AEF=0.
DO 25 J=1,N
V(J)=0.
AL(J)=0.
CONTINUE
DO 202 I=1,CT
DO 202 II=1,CT
BC(I,II)=0.
C1(I,II)=0.
CONTINUE
DO 371 J=1,N
DO 371 I=1,C
V(J)=V(J)+SV(J,I)
AL(J)=AL(J)+SL(J,I)
CONTINUE
DO 444 J=1,N
CONTINUE
GO TO 16
WRITE(44,9)
FORMAT(/,"SUCESSFUL CONVERGENT")
WRITE(44,200)IN
FORMAT(/,ITERATION NUMBER=',I30)
WRITE(44,2410)
FORMAT(4X,"FINAL VALUES OF FLOW RATES AND TEMPERATURE ARE:")
WRITE(44,2411)
FORMAT(4X,"VAPOR PHASE COMPONENT FLOW RATES ARE")
WRITE(44,2412)
FORMAT(4X,36("-"))
WRITE(44,2413)
FORMAT(4X,"COMPONENT NO.",10X,"STAGE NOS. ARE")
WRITE(44,4315)
FORMAT(4X,13("-"),10X,14("-"),/)
WRITE(44,2414)
FORMAT(26X,"1",12X,"2",12X,"3",12X,"4",12X,"5",12X,"6",12X,
      "7",12X,"8")

```

```

141 WRITE(44,2441)
141 FORMAT(4X,116(' '))
141 WRITE(44,4351)
141 FORMAT(//)
141 WRITE(44,3922)(I,(SV(J,I),J=1,N),I=1,CD)
141 FORMAT(4X,I3,7X,8(E10.4,3X)),//)
141 WRITE(44,1319)
141 FORMAT(//,4X,'LIQ. COMP. FLOW RATES ARE')
141 WRITE(44,2412)
141 WRITE(44,2413)
141 WRITE(44,4315)
141 WRITE(44,2414)
141 WRITE(44,2441)
141 WRITE(44,3922)(I,(SL(J,I),J=1,N),I=1,CD)
141 FORMAT(4X,4449)
141 FORMAT(//,4X,'VAPOR AND LIQUID RATE AND TEMPERATURE ARE',//)
141 WRITE(44,4467)
141 FORMAT(4X,420(' '))
141 WRITE(44,4468)
141 FORMAT(4X,'STAGE NUMBER',4X,'VAPOR RATE',4X,'LIQUID
141 RATE',4X,'TEMPERATURE')
141 WRITE(44,7679)
141 FORMAT(4X,12C(' '),4X,19(' '),4X,17(' ',''),4X,19(' ',''),/)
141 WRITE(44,122)(J,V(J),AL(JD,T(J),J=1,N))
141 FORMAT(8X,I3,5X,E19.8,4X,E17.8,4X,E19.8)
141 IFAIL=1
141 STOP
141 END
141 CORRECTED VERSION OF PRODUCT FORM OF INVERSE
141 A MATRIX IS TO BE INVERTED
141 INVERTED MATRIX IS TT
141 =====
141 SUBROUTINE GBI(A)
141 INTEGER CT
141 COMMON C/CT/N
141 DIMENSION A(CT,CT),TT(29,29),UI(29,29),T(29,29),ETA(29,29)
141 DO 1 I=1,CT
141 UI(I,I)=1.
141 CONTINUE
141 DO 5 K=1,CT
141 ETA(K,K)=1./A(K,K)
141 DO 4 I=1,CT
141 IF(I.EQ.K) GOTO 4
141 ETA(I,K)=-A(I,K)/A(K,K)
141 CONTINUE
141 DO 6 I=1,CT
141 ETA(I,K)=ETA(I,K)-UI(I,K)
141 CONTINUE
141 DO 7 I=1,CT
141 DO 7 J=1,CT
141 T(I,J)=UI(I,J)+ETA(I,K)*UI(K,J)
141 CONTINUE
141 DO 8 I=1,CT
141 DO 8 J=1,CT
141 ETA(I,J)=0.
141 IF(K.NE.1) GOTO 8
141 T(I,J)=T(I,J)
141 CONTINUE
141 DO 9 I=1,CT
141 DO 9 J=K,CT
141 DO 9 IJ=1,CT

```

```

ETA(I,J)=T(I,IJ)*A(IJ,J)+ETA(I,J)
CONTINUE
DO 10 I=1,CT
DO 10 J=1,CT
A(I,J)=ETA(I,J)
ETA(I,J)=0.
CONTINUE
IF(K.EQ.1) GOTO 5
DO 11 I=1,CT
DO 11 J=1,CT
DO 11 IJ=1,CT
ETA(I,J)=T(I,IJ)*TT(IJ,J)+ETA(I,J)
CONTINUE
DO 12 I=1,CT
DO 12 J=1,CT
TT(I,J)=ETA(I,J)
ETA(I,J)=0.
CONTINUE
CONTINUE
DO 21 I=1,CT
DO 21 J=1,CT
A(I,J)=TT(I,J)
CONTINUE
RETURN
END

SUBROUTINE MTMUL2(A,B)
INTEGER C,CT
COMMON C,CT,N
DIMENSION A(CT,CT),B(CT,CT),D(29,29)
DO 1 I=1,CT
DO 1 J=1,CT
DO 1 IJ=1,CT
D(I,J)=D(I,J)+A(I,IJ)*B(IJ,J)
CONTINUE
DO 2 I=1,CT
DO 2 J=1,CT
B(I,J)=D(I,J)
D(I,J)=0.
CONTINUE
RETURN
END

SUBROUTINE MTMUL1(A,B)
INTEGER C,CT
COMMON C,CT,N
DIMENSION A(CT,CT),B(CT),D(29)
DO 1 I=1,CT
DO 1 II=1,CT
D(I)=A(I,II)*B(II)+D(I)
CONTINUE
DO 2 I=1,CT
B(I)=D(I)
D(I)=0.
CONTINUE
RETURN
END

SUBROUTINE SUBMAT(B,C1)
INTEGER C,CT
COMMON C,CT,N
DIMENSION B(CT,CT),C1(CT,CT)
DO 1 I=1,CT
DO 1 J=1,CT

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```

B(I,J)=B(I,J)-C1(I,J)
CONTINUE
RETURN
END
SUBROUTINE ENL(T,EL)
INTEGER C,CT
COMMON C,CT,N
COMMON /A2/SC
DIMENSION EL(C),SC(14,4)
DO 1 I=1,C
EL(I)=SC(I,1)+SC(I,2)*T+SC(I,3)*T**2+SC(I,4)*T**3
CONTINUE
RETURN
END
SUBROUTINE DENL(T,EL)
INTEGER C,CT
COMMON C,CT,N
COMMON /A2/SC
DIMENSION EL(C),SC(14,4)
DO 1 I=1,C
EL(I)=SC(I,2)+2.*SC(I,3)*T+3.*SC(I,4)*T**2
CONTINUE
RETURN
END
SUBROUTINE ENV(T,EV)
INTEGER C,CT
COMMON C,CT,N
COMMON /A3/SE
DIMENSION EV(C),SE(14,4)
DO 1 I=1,C
EV(I)=SE(I,1)+SE(I,2)*T+SE(I,3)*T**2+SE(I,4)*T**3
CONTINUE
RETURN
END
SUBROUTINE DENV(T,EV)
INTEGER C,CT
COMMON C,CT,N
COMMON /A3/SE
DIMENSION EV(C),SE(14,4)
DO 1 I=1,C
EV(I)=SE(I,2)+SE(I,3)*2.*T+3.*SE(I,4)*T**2
CONTINUE
RETURN
END
SUBROUTINE DIST(T,AK)
INTEGER C,CT
COMMON C,CT,N
COMMON /A1/SA
DIMENSION AK(C),SA(14,4)
DO 1 I=1,C
AK(I)=T*(SA(I,1)+SA(I,2)*T+SA(I,3)*T**2+SA(I,4)*T**3)**3
CONTINUE
RETURN
END
SUBROUTINE DDIST(T,AKD)
INTEGER C,CT
COMMON C,CT,N
COMMON /A1/SA
DIMENSION AK(C),SA(14,4)
DO 1 I=1,C
AK(I)=(SA(I,1)+SA(I,2)*T+SA(I,3)*T**2+SA(I,4)*T**3)**3+3.*T*(
```

$1 \cdot SA(I,2) + 2 \cdot SA(I,3) \cdot T + 3 \cdot SA(I,4) \cdot T^2 \cdot (SA(I,1) + SA(I,2) \cdot T$   
 $2 \cdot SA(I,3) \cdot T^2 + SA(I,4) \cdot T^3)^2$

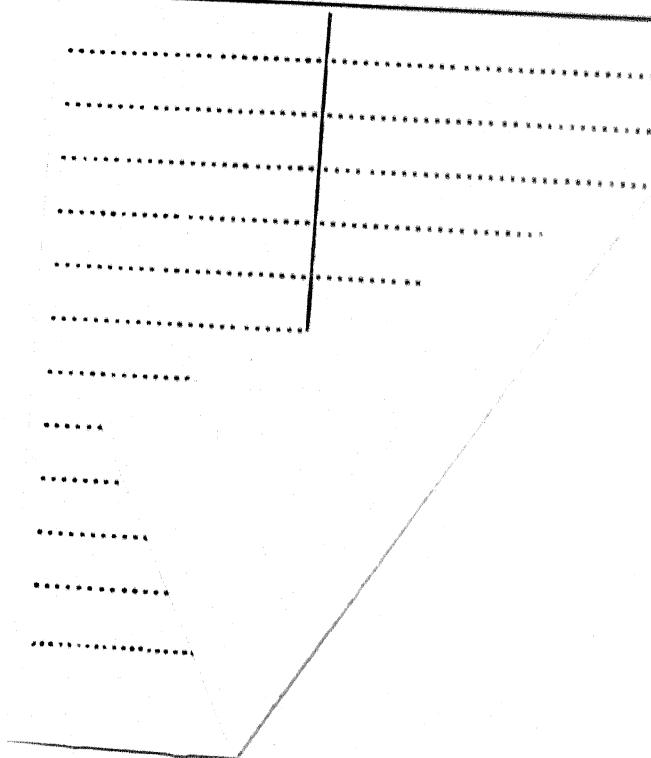
CONTINUE  
RETURN  
END

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